



International RELAP5 Users Group Meeting And Training Seminars

# **Improvements to PHISICS/RELAP5-3D<sup>©</sup> Capabilities for Simulating HTGRs – NK Adaptive time step implementation**

Idaho Falls, ID October 7, 2016

P.Balestra, A. Alfonsi, G. Strydom, C. Rabiti, F. Giannetti, G. Caruso



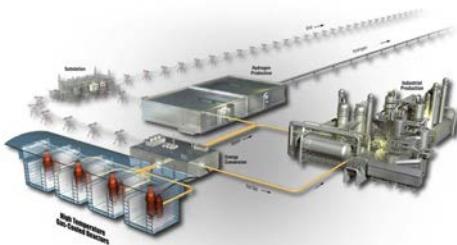
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- ❑ Code & models
- ❑ Decoupling scheme
- ❑ Adaptive time step
- ❑ Conclusions



# The Objective

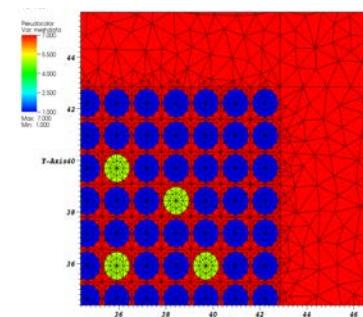
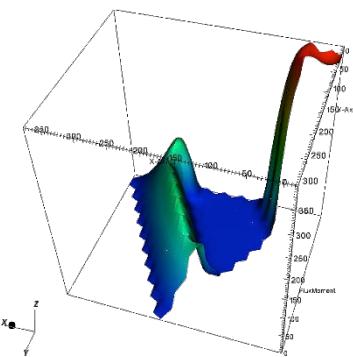
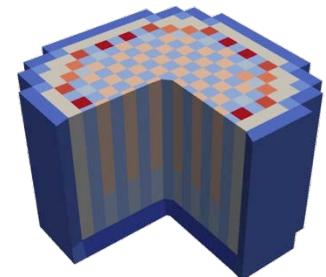
- ❑ Improvement of the **PHISICS/RELAP5-3D<sup>©</sup>** coupling scheme to allow the **NK** code to use a time step different from the **TH** one.
- ❑ Introduce a control logic that calculate the next **NK time step** size to keep the error of the flux solution under a certain tolerance.
- ❑ Test the new coupling scheme on the **High Temperature Test Reactor (HTTR)** model for the **LOFC** transient in order to speed up the simulations and validate the code modifications.





# Code & Models

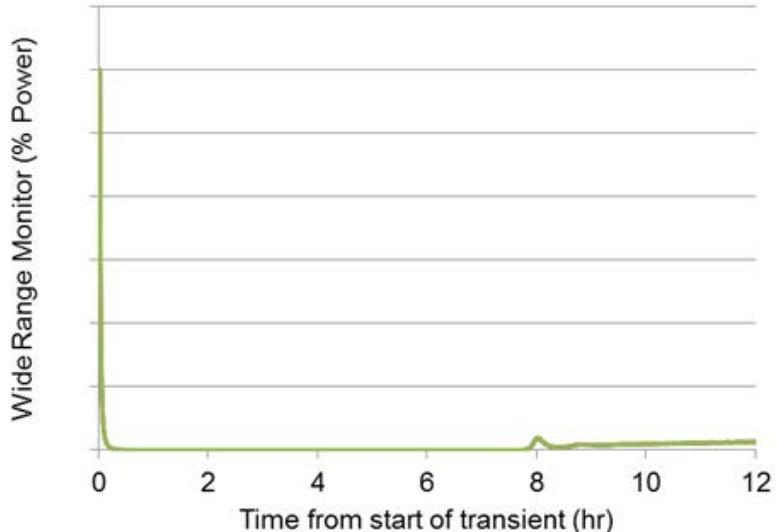
- **PHISICS** code modules overview
  - **INSTANT**: Transport/diffusion nodal solver, spherical harmonics based methodology, Second order formulation:
    - Unlimited number of energy group.
    - Spatial and angular discretization order up to 33
    - Cartesian 2/3D, Hex 2/3D, Unstructured Triangular, Wedges.
    - Adjoint calculations.
  - **MRTAU**: Bateman solver, CRAM, depletion evolution.
  - **MIXER**: Cross section manager, micro, macro or mixed, Unlimited number of tabulation parameters.
  - **COUPLING**: **RELAP5-3D<sup>©</sup>** coupled, for steady state and transient simulations.



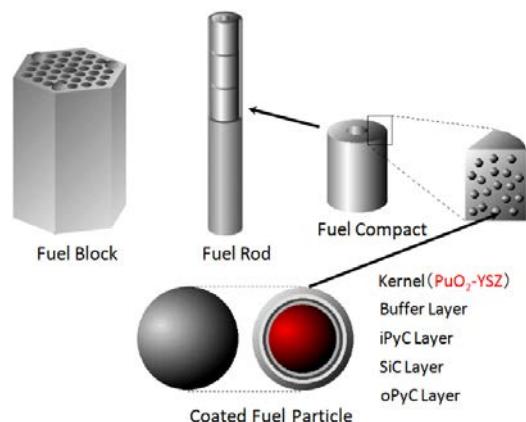


# Code & Models

- The HTTR and LOFC transient
  - December 2010, JAEA performed a LOFC, with automatic reactor trip circuitry disabled.
  - When the forced flow stopped, the fuel temperature increased → negative reactivity → sub-critical within the first minute.
  - Critical again after 8h for the Xe<sup>135</sup> decay



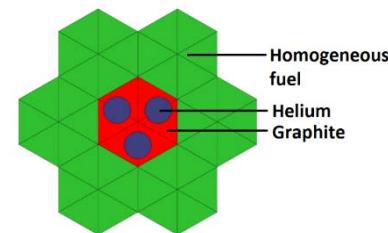
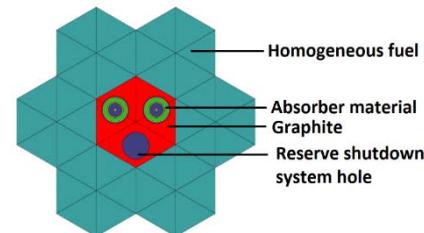
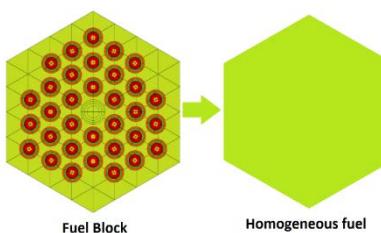
| Reactor main parameters    |                       |
|----------------------------|-----------------------|
| Power                      | 30 MW                 |
| Coolant                    | Helium                |
| Primary pressure           | 2.774 MPa             |
| Average power density      | 2.5 W/cm <sup>3</sup> |
| Core diameter              | 2.9 m                 |
| Outlet coolant temperature | 320°C                 |
| Inlet coolant temperature  | 180°C                 |





# Code & Models

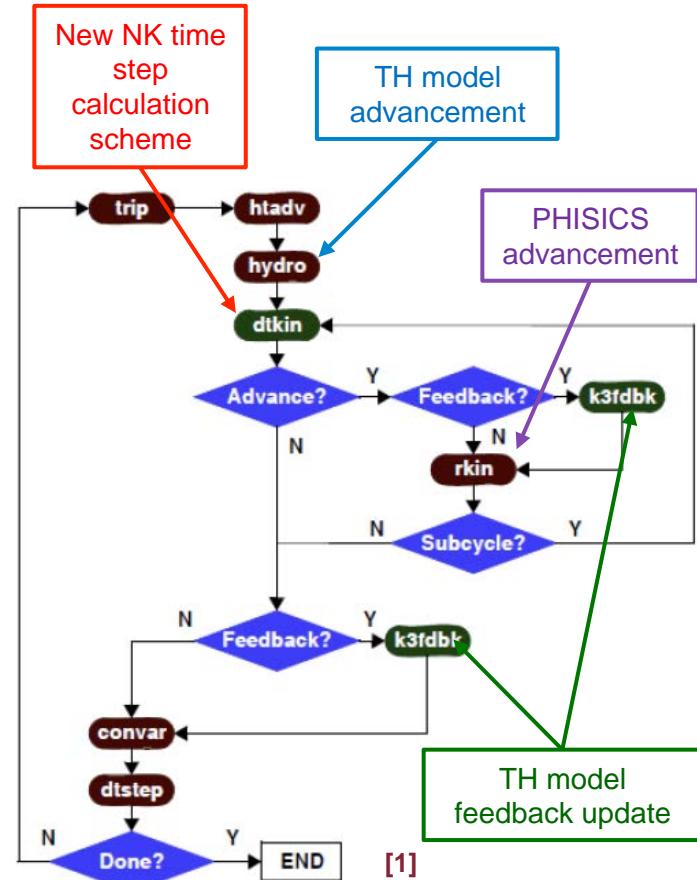
- HTTR 3D NK and TH model
  - TH model: One TH channel for each radial ring + conduction and radiation model.
  - NK model: 3D Hex assembly by assembly nodalization with 5 axial meshes for the active zone
  - XSec: mixed XSec generated using DRAGON5
    - Macro XSec for the FUEL.
    - Micro XSec with  $Xe^{135}$  and  $I^{135}$ .
    - Tabulated respect to Fuel, Moderator temperature, and  $Xe^{135}$  concentration



# Decoupling scheme

## □ Decoupling scheme

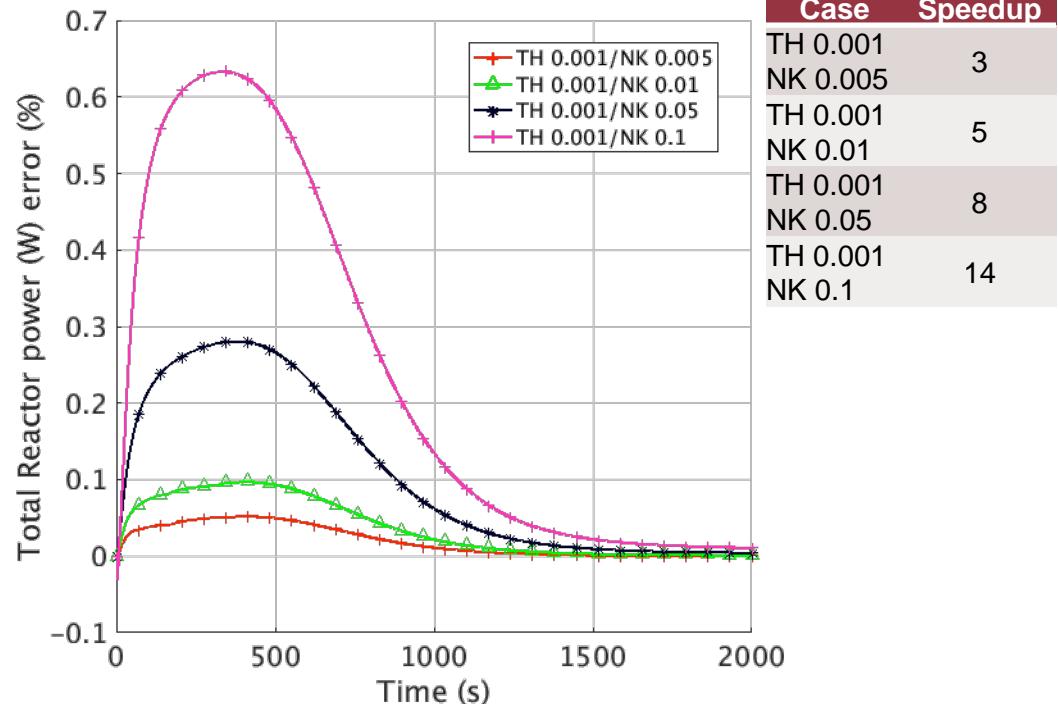
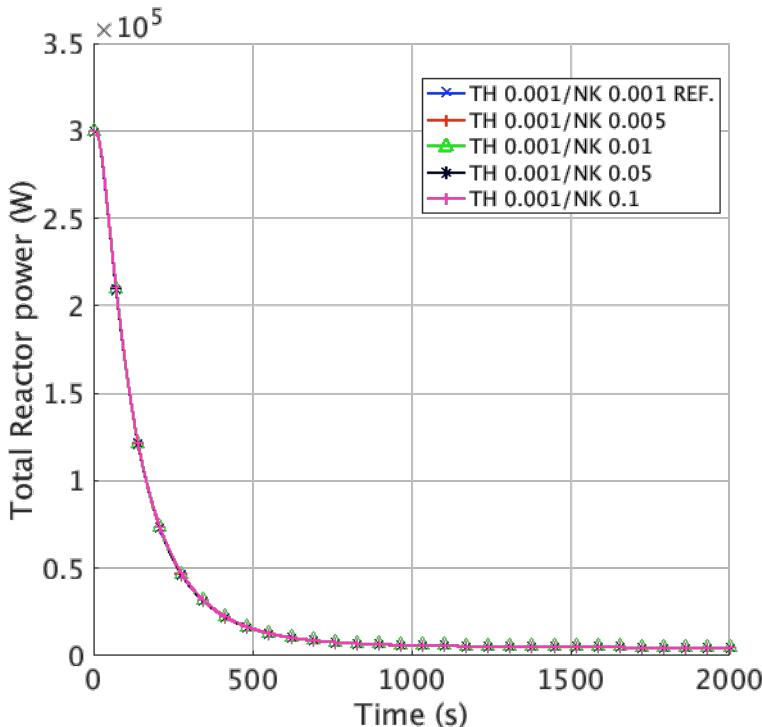
- The **RELAP5-3D<sup>©</sup>** decoupling scheme developed for **NESTLE** has been used → **Minor modifications** applied to the **PHISICS** code in order to use the new NK time step for **MRTAU** (depletion) and for the time evolution scheme.
- To verify the functionality of the modifications with a simplified model, using the same **PHISICS** modules → **Reduced** version of **HTTR** model → one ring and one NK reflected assembly 15 axial nodes.



[1] D.Barber, "RELAP5-3D Model Improvement", International RELAP5 Users Group Meeting, Sun Valley, Idaho, 2012

# Decoupling scheme

- ❑ Constant NK Time step results for time step decoupling scheme testing
  - Reference solution  $\Delta t_{NK} = \Delta t_{TH} = 1e-3s$  for 2000 s transient (**2E+6 iterations**)
  - The  $\Delta t_{TH}$  has been kept to  $1e-3s$  to ensure that the TH solution is fully converged and does not introduce error in the calculations.



**WARNING: THERE IS NO CONTROL ON THE NK SOLUTION ERROR!!!**



# Adaptive time step

## □ Adaptive time step calculation scheme:

$$\partial \phi_{\downarrow r}^{\uparrow g} / \partial t |_{\downarrow t=t_{\downarrow n}} = \phi_{\downarrow r}^{\uparrow g}(n) - \phi_{\downarrow r}^{\uparrow g}(n-1) / \Delta t_{\downarrow n} + e_{\downarrow \phi}^{\uparrow}(n)$$

$$e_{\downarrow \phi}^{\uparrow}(n) = \Delta t_{\downarrow n} / 2 \partial \tau^2 \phi_{\downarrow r}^{\uparrow g} / \partial t^{\uparrow 2} |_{\downarrow t=t_{\downarrow n} + O(\Delta t_{\downarrow n}^{\uparrow 2})} \\ \leq \tau$$



Predicted Time step

$$\Delta t_{\downarrow p} \leq \sqrt{2} \tau / \partial \tau^2 \phi_{\downarrow r}^{\uparrow g} / \partial t^{\uparrow 2} |_{\downarrow t=t_{\downarrow n}}$$

Additional constraints

- 1)  $0.001 \leq \Delta t_{\downarrow p} \leq 2.0$  s
- 2)  $\Delta t_{\downarrow p}$  rational multiple of the  $\Delta t_{\downarrow TH}$

### Methodology 1 (M1)

$$\partial \tau^2 \phi_{\downarrow r}^{\uparrow g} / \partial t^{\uparrow 2} |_{\downarrow t=t_{\downarrow n}} \approx \Delta t_{\downarrow n-1} \phi_{\downarrow r}^{\uparrow g}(n) - (\Delta t_{\downarrow n-1} + \Delta t_{\downarrow n}) \phi_{\downarrow r}^{\uparrow g}(n-1) + \Delta t_{\downarrow n} \phi_{\downarrow r}^{\uparrow g}(n-2) / \Delta t_{\downarrow n-1} \Delta t_{\downarrow n} (\Delta t_{\downarrow n-1} + \Delta t_{\downarrow n})$$

### Methodology 2 (M2)

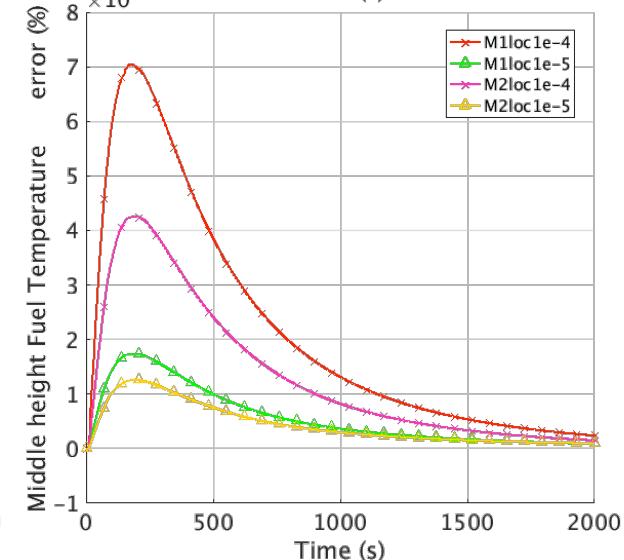
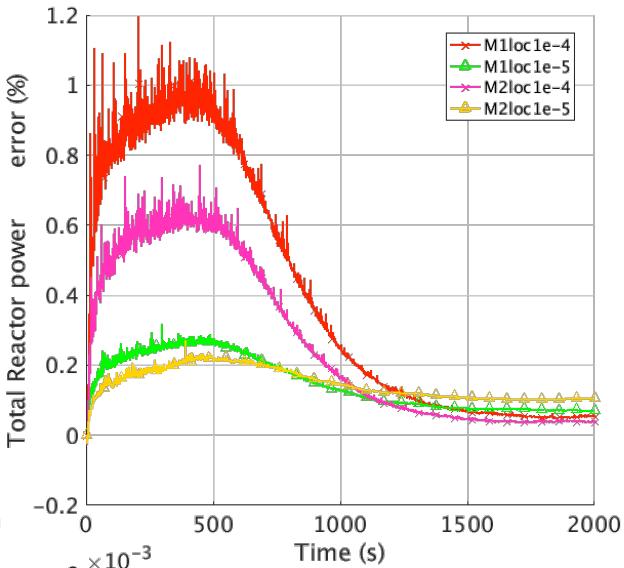
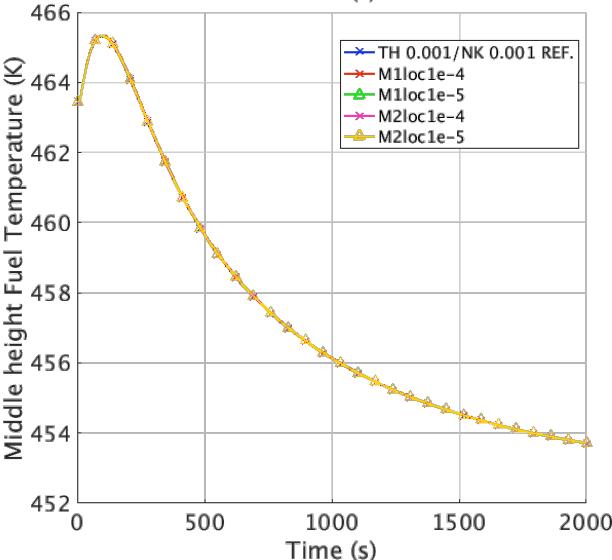
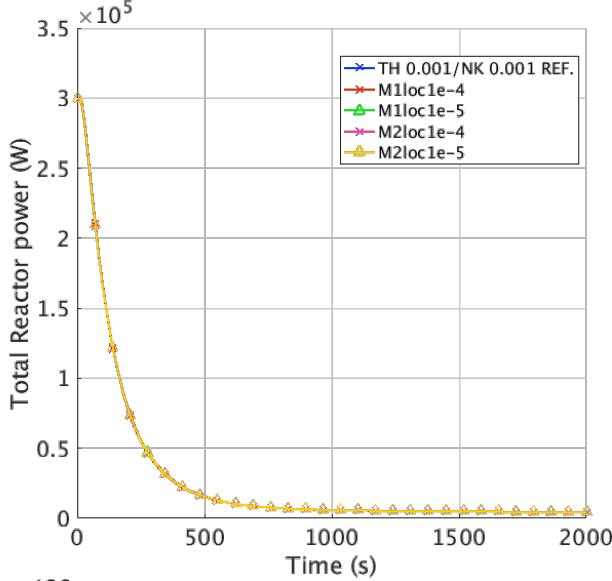
[2]

$$\partial \tau^2 \phi_{\downarrow r}^{\uparrow g} / \partial t^{\uparrow 2} |_{\downarrow t=t_{\downarrow n}} \approx \Delta t_{\downarrow n-1} \phi_{\downarrow r}^{\uparrow g}(n) - (\Delta t_{\downarrow n-1} + \Delta t_{\downarrow n}) \phi_{\downarrow r}^{\uparrow g}(n-1) + \Delta t_{\downarrow n} \phi_{\downarrow r}^{\uparrow g}(n-2) / \Delta t_{\downarrow n} \Delta t_{\downarrow n} \Delta t_{\downarrow n-1}$$

[2] M. W. Hackemack, J. M. Pounds, "Implementation of an a priori time step estimator for the multigroup neutron diffusion equation in asynchronously coupled RELAP5-3D", PHYSOR 2014, The Westin Miyako, Kyoto, Japan, 2014

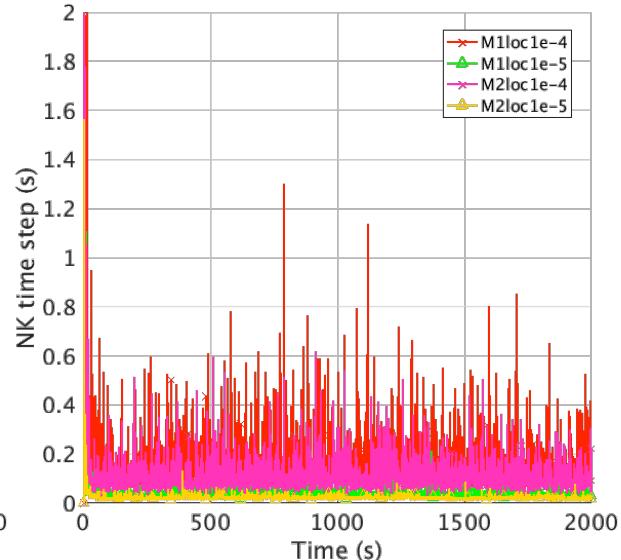
# Adaptive time step

M1 vs M2 results with local tolerance:



| Case                  | Speedup |
|-----------------------|---------|
| M1loc $\epsilon=1e-4$ | 18      |
| M1loc $\epsilon=1e-5$ | 7       |
| M2loc $\epsilon=1e-4$ | 12      |
| M2loc $\epsilon=1e-5$ | 6       |

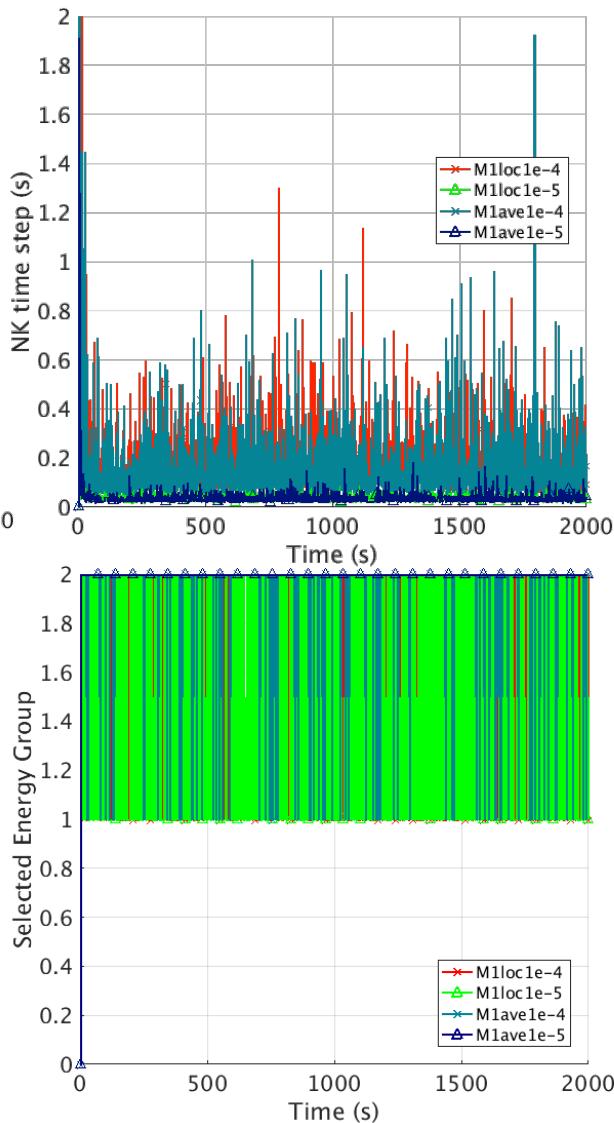
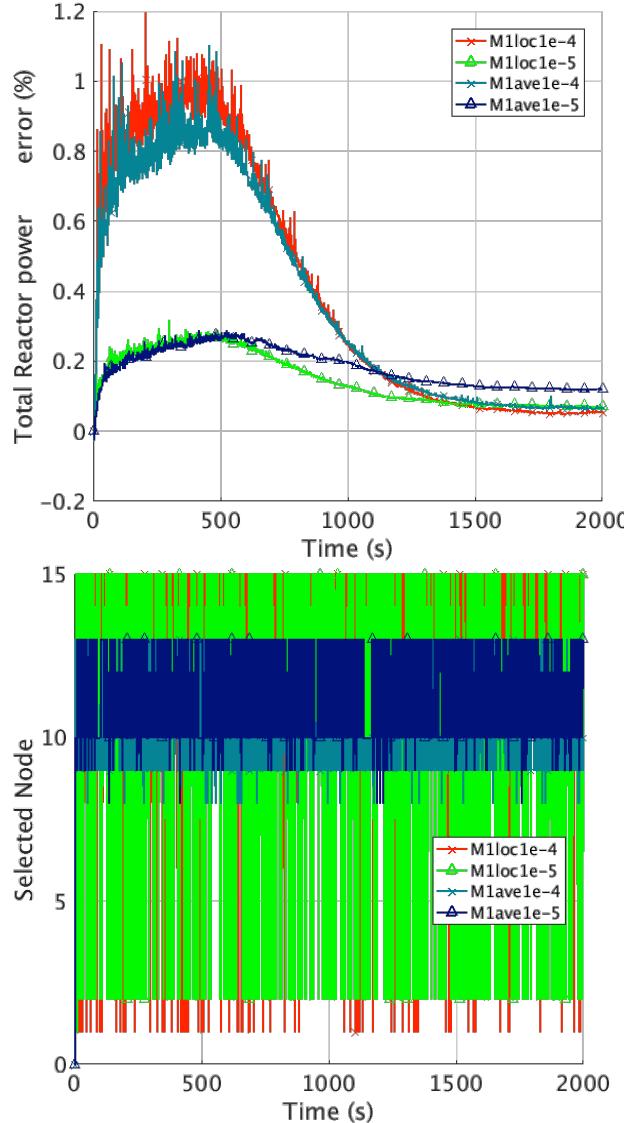
Local Tolerance  
 $\Delta t \downarrow n = \min(\sqrt{2\tau} / \partial t \downarrow 2 \phi \downarrow r \uparrow g / \partial t \downarrow 2 / \uparrow - 1)$   
 $\tau = \epsilon \phi \downarrow r \uparrow g$





# Adaptive time step

## Average tolerance vs local tolerance results



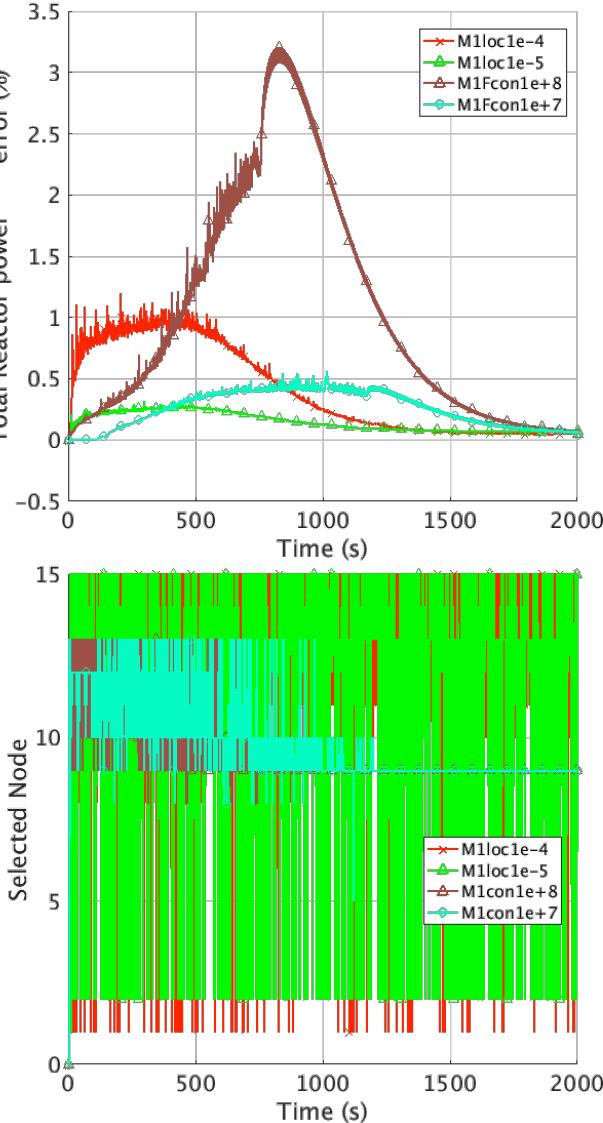
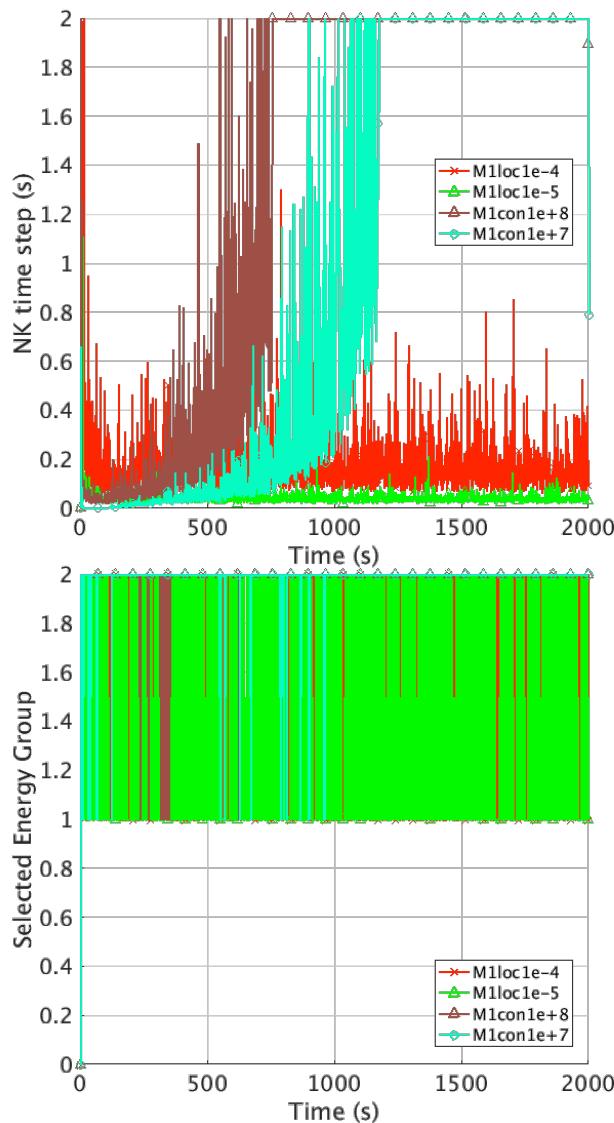
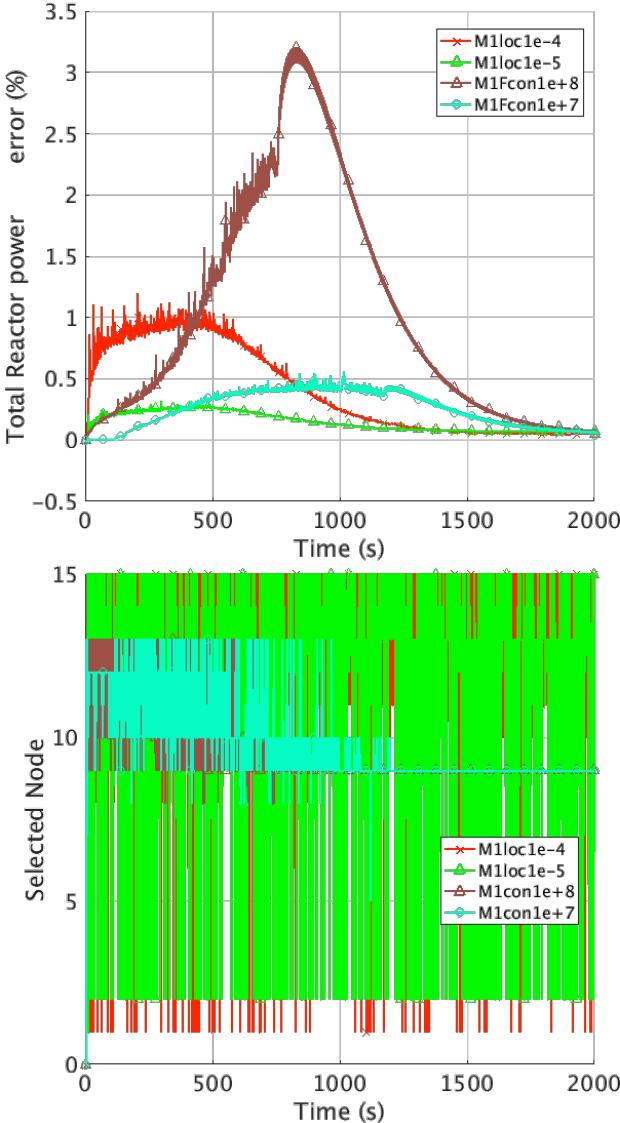
| Case                  | Speedup |
|-----------------------|---------|
| M1loc $\epsilon=1e-4$ | 18      |
| M1loc $\epsilon=1e-5$ | 7       |
| M1ave $\epsilon=1e-4$ | 15      |
| M1ave $\epsilon=1e-5$ | 7       |

Average flux Tolerance  
 $\Delta t \downarrow n = \min(\sqrt{2\tau} / \partial t \downarrow 2 \phi \downarrow r \uparrow g / \partial t \downarrow 2 / \uparrow -1)$   
 $\tau = \epsilon \phi$

N.B. the tolerance is proportional to average flux but the second derivative is still calculated in each node and energy group

# Adaptive time step

## Constant tolerance vs local tolerance results



| Case                     | Speedup |
|--------------------------|---------|
| M1loc $\varepsilon=1e-4$ | 18      |
| M1loc $\varepsilon=1e-5$ | 7       |
| M1con $\varepsilon=1e+8$ | 33      |
| M1con $\varepsilon=1e+7$ | 10      |

Constant Tolerance

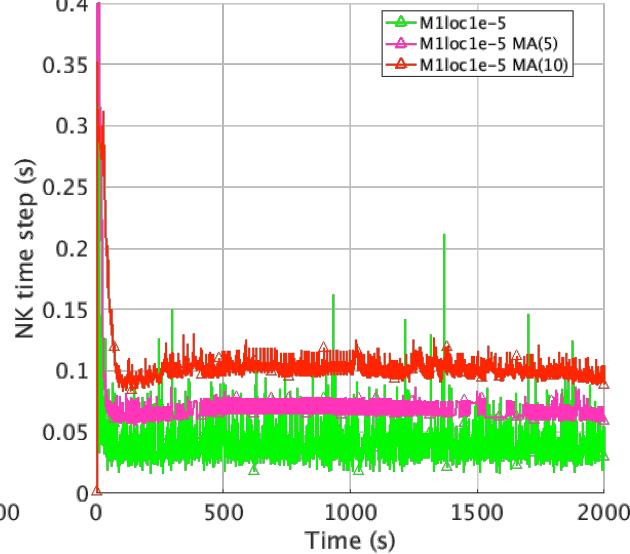
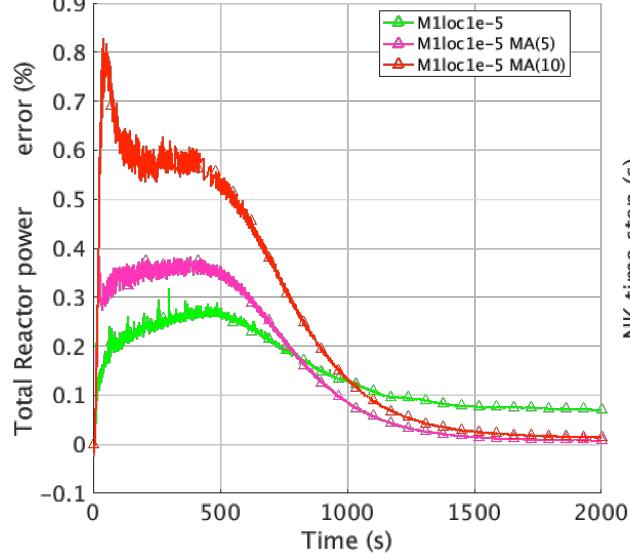
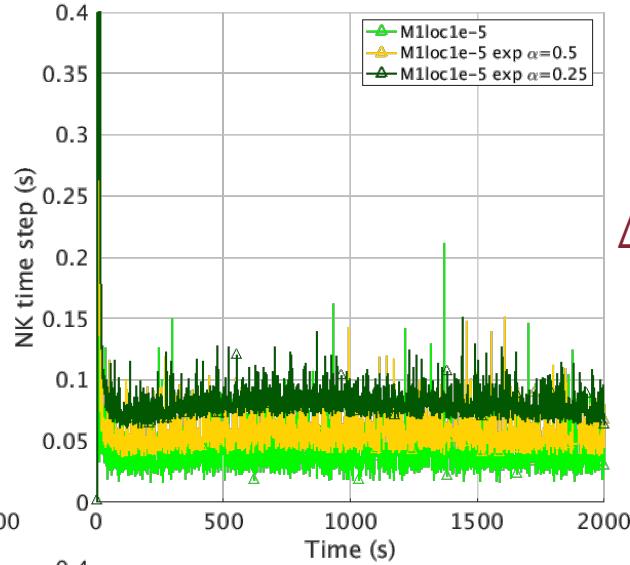
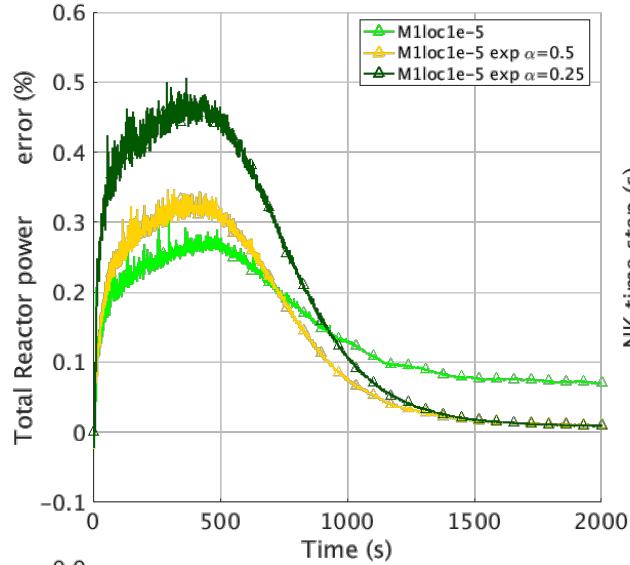
$$\Delta t \downarrow n = \min(\sqrt{2\tau} / \partial t \downarrow 2 \phi \downarrow r \uparrow g / \partial t \downarrow 2 / \uparrow -1)$$

$$\tau = \varepsilon [n/cm^2/s]$$

N.B. the tolerance is proportional to average flux but the second derivative is still calculated in each node and energy group.

# Adaptive time step

## □ Moving average (MA) and Exponential smoothing on NK Δt prediction



Exponential smoothing

$$\Delta t \downarrow n = \Delta t \downarrow n-1 (1-\alpha) + \alpha \Delta t \downarrow n$$

Moving average MA(N)

$$\Delta t \downarrow n = \sum_{i=1}^N \Delta t \downarrow n - i$$

| Case                              | Speedup |
|-----------------------------------|---------|
| M1loc $\epsilon=1e-5$             | 7       |
| M1loc $\epsilon=1e-5 \alpha=0.5$  | 8       |
| M1loc $\epsilon=1e-5 \alpha=0.75$ | 11      |
| M1loc $\epsilon=1e-5$ MA(5)       | 10      |
| M1loc $\epsilon=1e-5$ MA(10)      | 14      |



# Conclusion & future steps

- ❑ The **RELAP5-3D<sup>©</sup>** decoupling scheme has been successfully modified and verified for the **PHISICS** code. All the **PHISICS** modules used in the **HTTR** model are now compatible with the new decoupling scheme.
- ❑ **Two** different Methodologies for the flux error estimation has been introduce. **Three** different kind of tolerance can be used to control the flux error trough the time step size. **Two** smoothing techniques are available to reduce the time step noise.
- ❑ More than **100** run with a simplified version of the **HTTR** model has been performed to test the best combination of **methodology**, **tolerance definition**, and **smoothing**.
- ❑ Future steps:
  - Test the modifications on the **full HTTR** model and the full **LOFC** (>40000 s)
  - Implement a **third methodology** for the time step prediction based on an more stable implicit scheme developed in [3].
  - Test the possibility of using some “**hybrid methodology**” using different methodology simultaneously. Introduce the **flux extrapolation** option.
  - Implement the **quasi-static** approach for very long transients (>1d).

[3] C.Rabiti, “Modelling of Fast Neutron Transients in an Accelerator Driven System”, IKE, 2007



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# New RELAP5-3D Lead and LBE thermophysical properties implementation for safety analysis of Gen IV reactors

Idaho Falls, ID October 7, 2016

P.Balestra, F. Giannetti, G. Caruso, A. Alfonsi



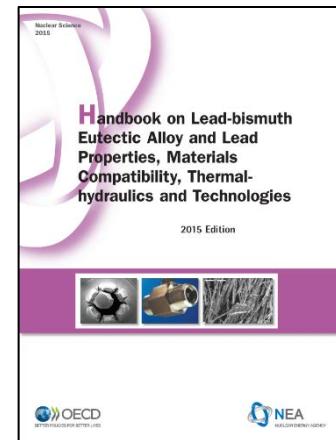
# Contents

- ❑ The objective
- ❑ Thermophysical property comparison
- ❑ The soft sphere model
- ❑ Practical cases calculation and comparison
- ❑ Conclusions



# The Objective

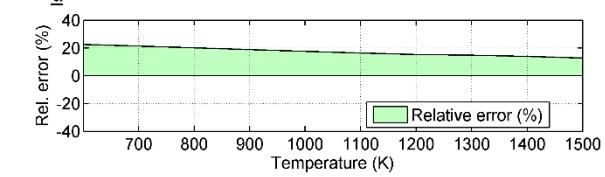
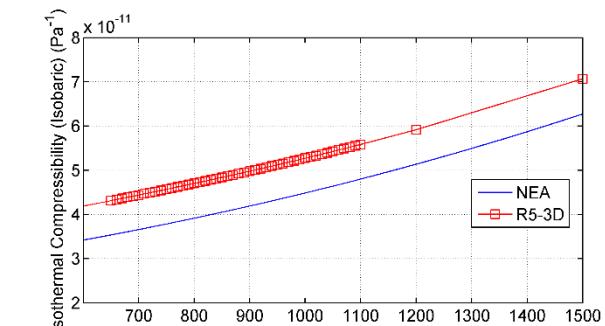
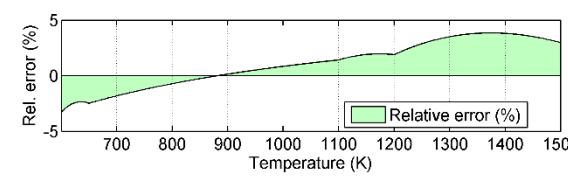
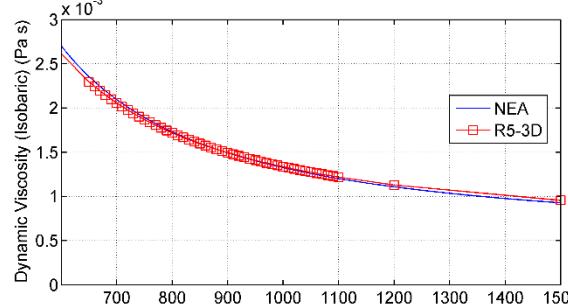
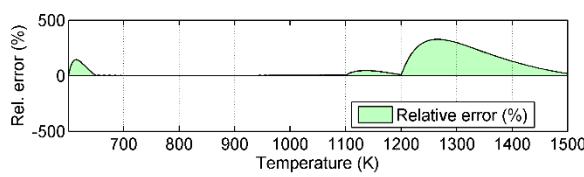
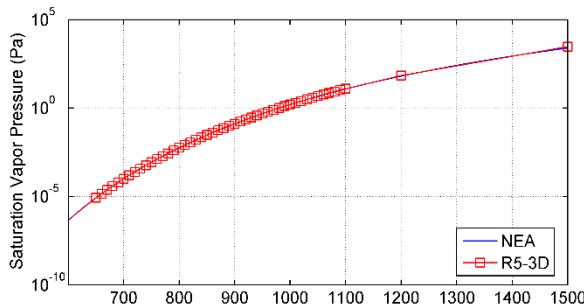
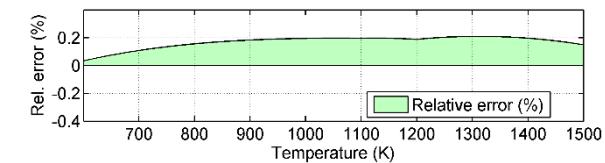
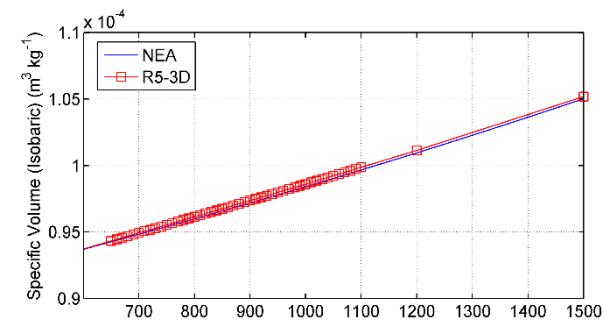
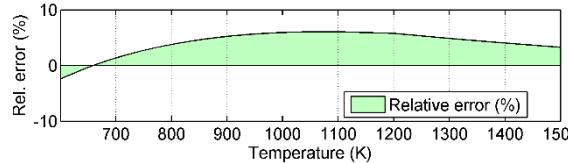
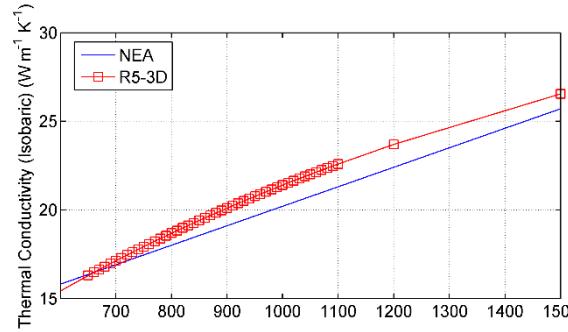
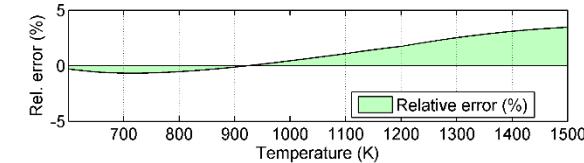
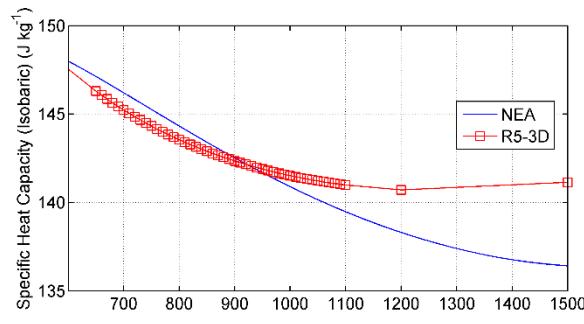
- ❑ Compare the RELAP5-3D<sup>©</sup> Lead and LBE thermophysical properties with the new one proposed in the 2015 NEA handbook. 
- ❑ Generate new thermophysical property files for LBE and Lead using a set of equation of state specific for the liquid metals fitted on the new NEA properties.
- ❑ Test and compare the effect of the new properties on the main parameters of a simple RELAP5-3D<sup>©</sup> model.





# Thermophysical Property comparison

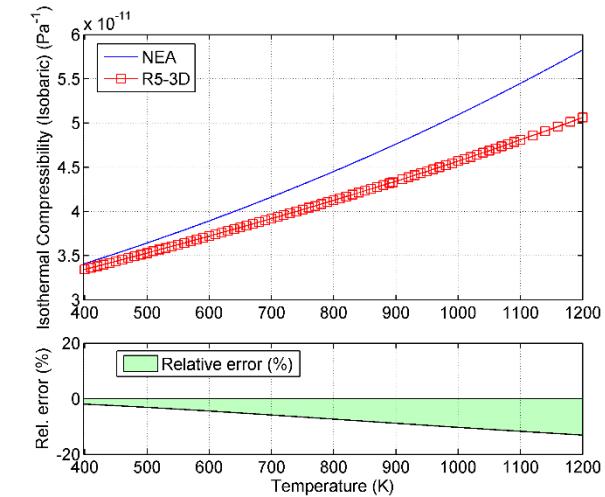
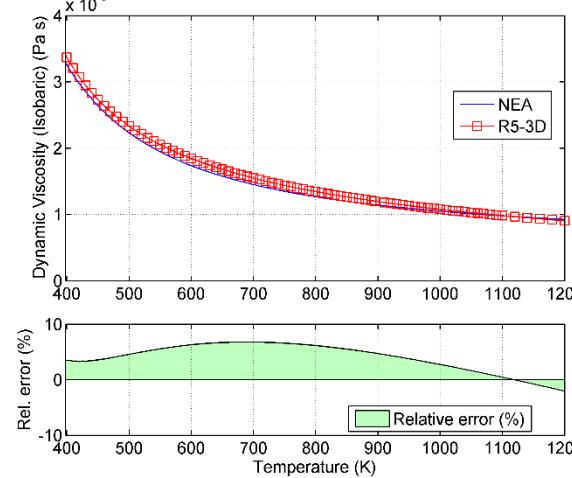
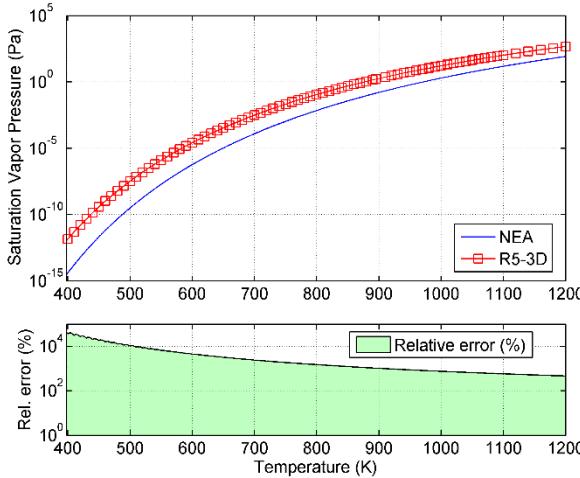
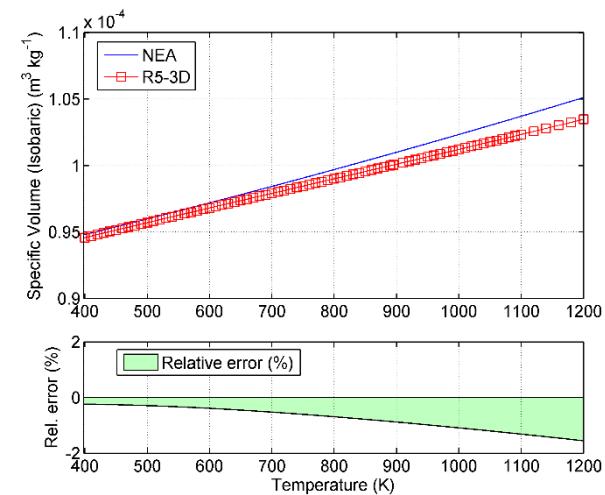
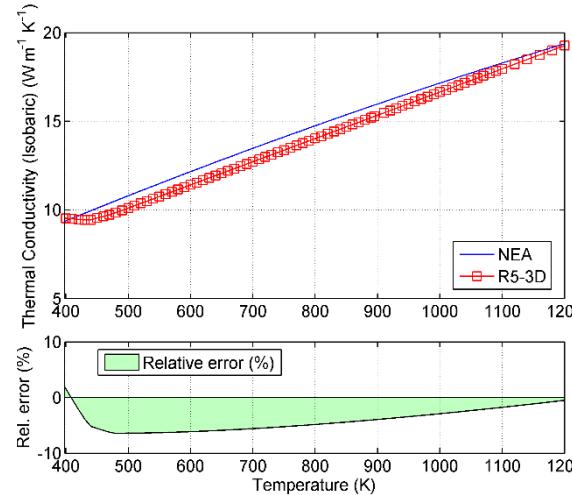
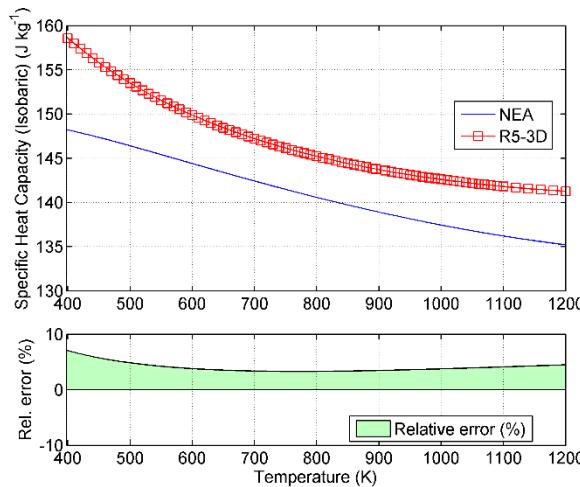
## □ Lead thermophysical properties R5-3D vs NEA 2015:





# Thermophysical Property comparison

## □ LBE thermophysical properties R5-3D vs NEA 2015:





# The soft sphere model

## □ Soft sphere model parameter optimization



Parameter to be optimized  
 $(n, m, Q, \sigma, \varepsilon, T)$



Error function definition

### MEASURED DATA

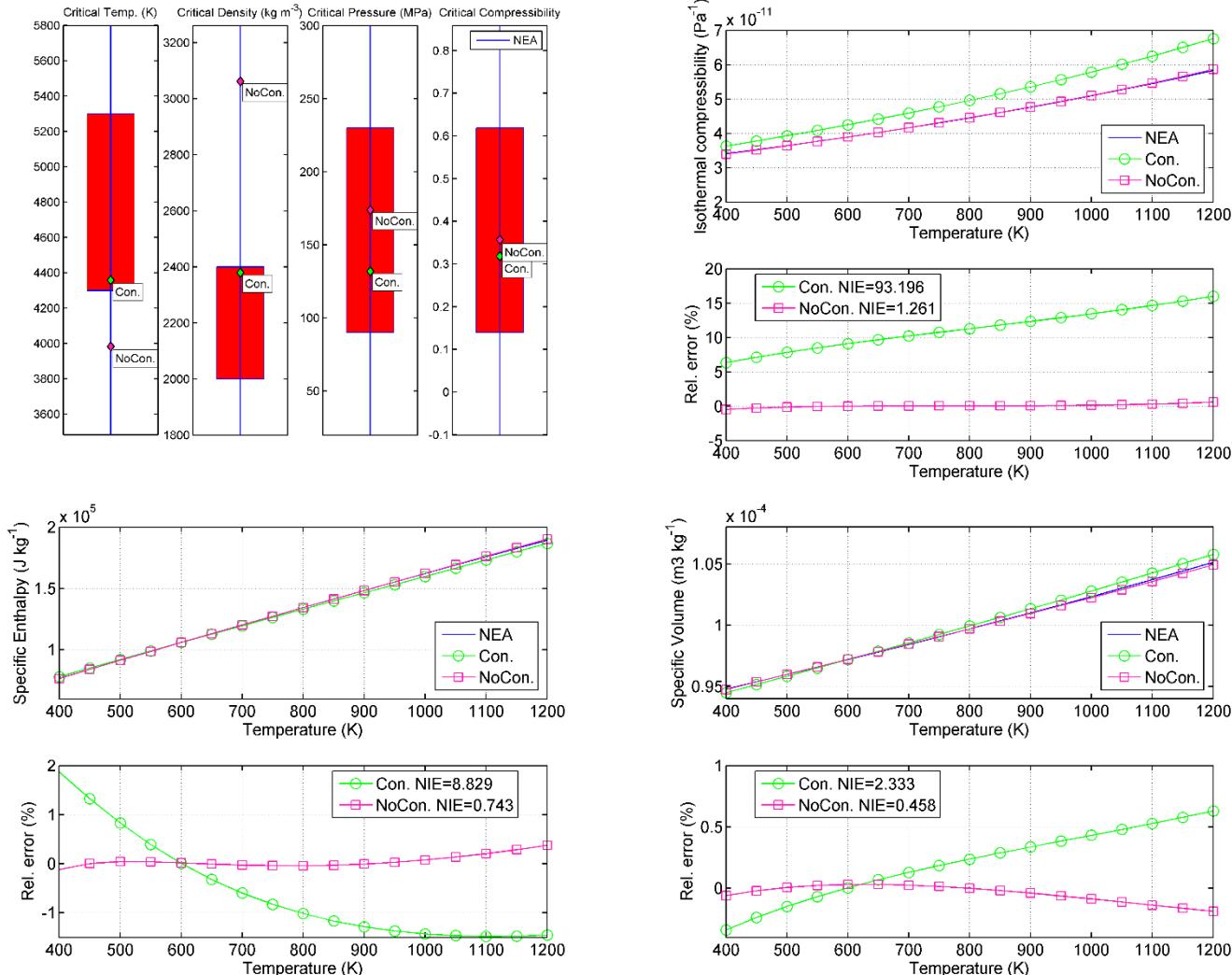
- Specific volume ( $i=1$ )
  - Specific enthalpy ( $i=2$ )
  - Isothermal compressibility ( $i=3$ )
- N.B available only for atmospheric pressure





# The soft sphere model

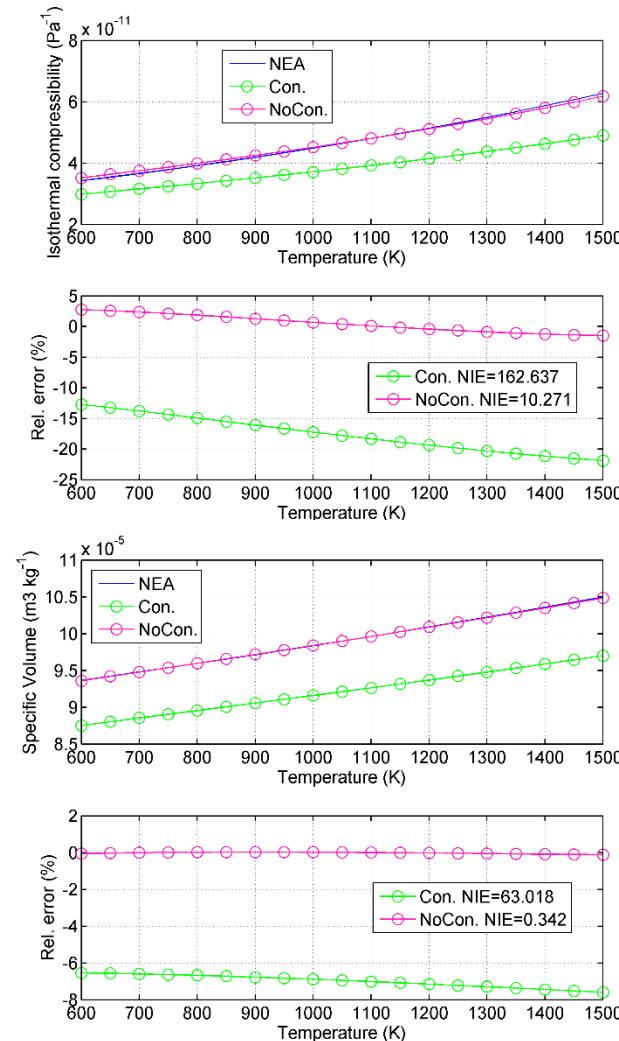
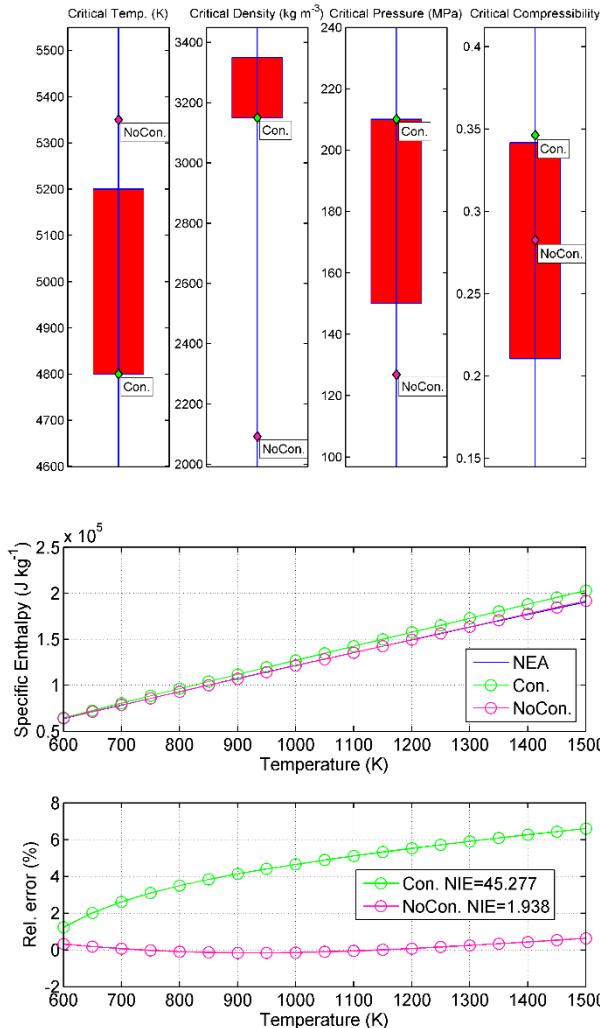
## Lead soft sphere model parameter optimization





# The soft sphere model

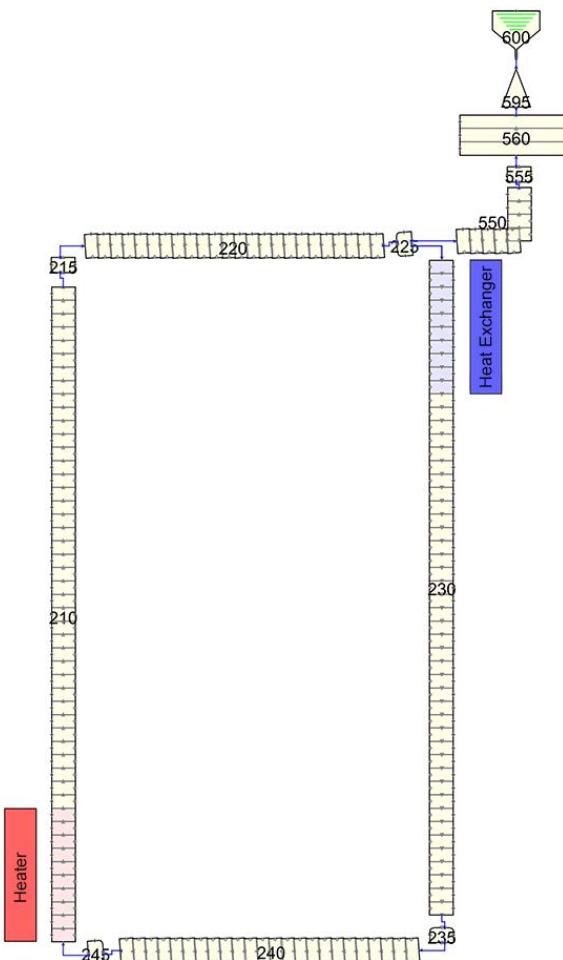
## LBE soft sphere model parameter optimization





# Practical cases calculation

## □ Simple natural circulation RELAP5-3D<sup>©</sup> model



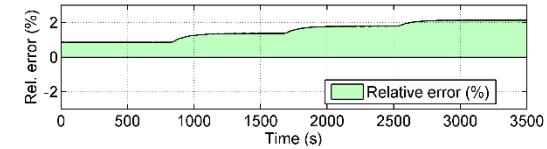
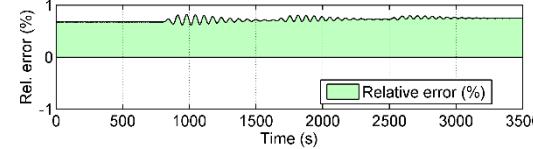
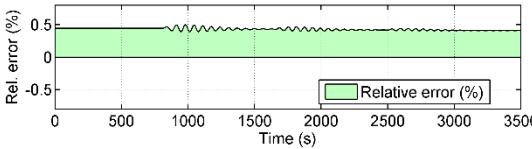
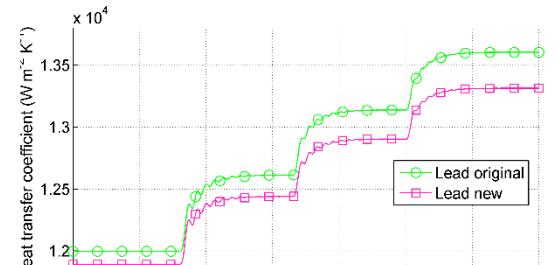
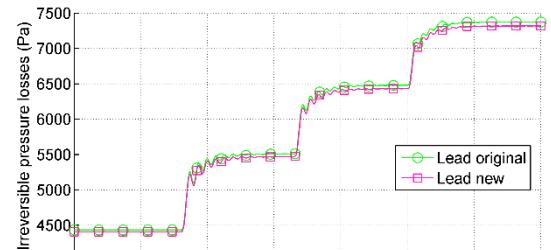
| Parameter                                   | Unit           | Value                    |
|---|----------------|--------------------------|
| Flow area                                   | m <sup>2</sup> | 9.348 · 10 <sup>-3</sup> |
| Absolute roughness                          | m              | 10 <sup>-5</sup>         |
| Heater steady state Power                   | kW             | 200.0                    |
| Heated section length                       | m              | 2.0                      |
| Heat sink wall temperature                  | K              | 610.0                    |
| Heat exchanger section length               | m              | 2.0                      |
| Heat exchanger area                         | m <sup>2</sup> | 0.686                    |
| Heat exchanger wall thickness               | m              | 2.5 · 10 <sup>-3</sup>   |
| Gas plenum pressure                         | Pa             | 2.0 · 10 <sup>5</sup>    |
| Vertical pipes length                       | m              | 10.0                     |
| Horizontal pipes length (4° vertical angle) | m              | 5.0                      |
| Expansion tank volume                       | m <sup>3</sup> | 0.36                     |
| Expansion tank height                       | m              | 0.6                      |
| Expansion tank level                        | m              | 0.3                      |



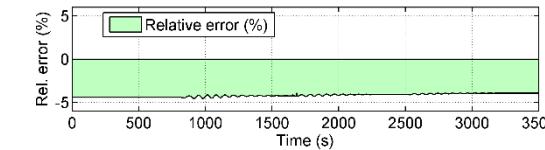
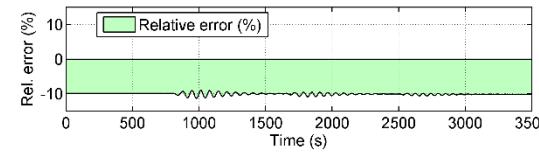
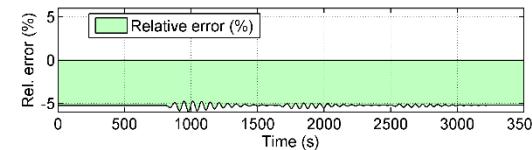
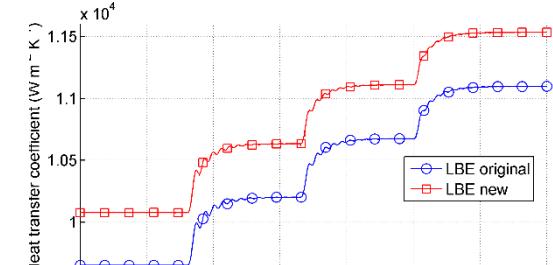
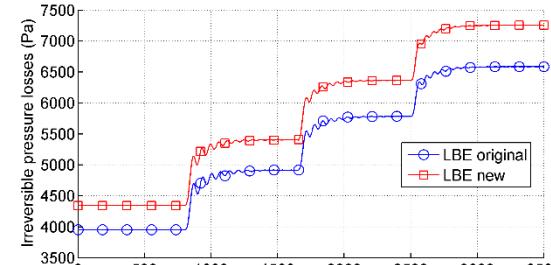
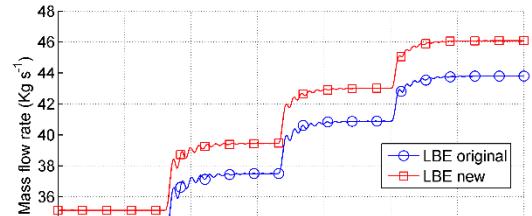
# Thermophysical Property comparison

- Lead and LBE Natural circulation loop main parameter comparison.

Lead



LBE





# Conclusion & future steps

- ❑ Full comparison between the original R5-3D thermophysical properties and the NEA recommended ones has been reported for two heavy liquid metals, **LBE** and **Lead**
- ❑ A simple NC system has been used to compare the effect on the TH model main parameters.
- ❑ **Lead** properties show a limited discrepancy.
- ❑ **LBE** properties show a significant discrepancy, therefore further investigations and validation using experimental data should be performed.
- ❑ The future activities will be devoted to find an **optimal pressure and temperature grid** to minimize the numerical issues during the calculations and to the validation of the new thermophysical properties using experimental data.



# Thank you for your attention !!!