Nuclear Reactor Sustainment and Expanded Deployment

| Abdalla Jaoude | Demonstrating Fuel | | |
|---|--|--|--|
| Boone Beausoleil | Passive Strain Meas | | |
| Brelon May | Accelerating pathwa | | |
| Chao Jiang | Machine Learning I | | |
| Cheng Sun | An Innovative Appro | | |
| Chuting Tsai | In situ positron ann | | |
| David Frazer | An accelerated asse | | |
| Fidelman Dillemanne | A combinatorial Mc | | |
| Fiueima Di Lemma | evolution in metalli | | |
| Jeren Browning | Unattended Operat | | |
| Kyle Gamble | Modeling and Meas | | |
| Kyle Gamble | High-fidelity multise | | |
| | element modeling | | |
| Mauricio Tano Retamales | Thermochemical me | | |
| Mohammad Abdo | Accelerated techno | | |
| Nedim Cinhiz | Informative Design | | |
| | mormative Design | | |
| Som Dhulinala | Accelerating and Im | | |
| Som Dhulipala | Accelerating and Im and Deployment of | | |
| Stofano Torlizzi | Accelerating and Im and Deployment of Development of Mu | | |
| Som Dhulipala Stefano Terlizzi | Accelerating and Im and Deployment of Development of Mu hydrides-moderated | | |
| Som Dhulipala Stefano Terlizzi Steven Prescott | Accelerating and Im and Deployment of Development of Mu hydrides-moderated Quantitative Reliabi | | |
| Som Dhulipala Stefano Terlizzi Steven Prescott Trishelle Copeland- | Accelerating and Im and Deployment of Development of Mu hydrides-moderated Quantitative Reliabi | | |
| Som Dhulipala Stefano Terlizzi Steven Prescott Trishelle Copeland- Johnson | Accelerating and Im and Deployment of Development of Mu hydrides-moderated Quantitative Reliabi | | |
| Som Dhulipala Stefano Terlizzi Steven Prescott Trishelle Copeland- Johnson | Accelerating and Im and Deployment of Development of Mu hydrides-moderated Quantitative Reliabi Characterizing corro Scalable Framework | | |
| Som Dhulipala Stefano Terlizzi Steven Prescott Trishelle Copeland- Johnson Vivek Agarwal | Accelerating and Im and Deployment of Development of Mu hydrides-moderated Quantitative Reliabi Characterizing corro Scalable Framework Microreactors | | |

www.inl.gov

Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517."

led-Salt Irradiation Capability to Support Reactor Deployment surements for Experiments in Radiation Environments vays to actinide materials discovery through combinatorial deposition nteratomic Potentials for Radiation Damage and Physical Properties in Model Fluorite Systems oach for Accelerated Irradiation Studies of Materials nihilation spectroscopy for characterizing irradiation induced defects essment of the creep mechanisms in uranium zirconium model alloys odeling and Simulation and Separate Effect Test approach to investigate unknown microstructural ic fuel pin

tion through Digital Twin Innovations

surement of Gas Transport in Nuclear Fuels

cale model development for accelerated fuel qualification using finite element-informed discrete

odeling of flow-accelerated corrosion in Molten Salt Reactors logy development through new extrapolation and validation methods of High-Temperature Metal Hydride Moderators in Microreactors nproving the Reliability of Low Failure Probability Computations to Support the Efficient Safety Evaluation Advanced Reactor Technologies

ultiphysics Object Oriented Simulation Environment based capabilities to model hydrogen migration in d microreactors

ility Analysis for Unattended Operation of Fission Batteries

osion mechanisms of structural alloys in actinide-based molten chloride salt

k of Hybrid Modeling with Anticipatory Control Strategy for Autonomous Operation of Modular and

ition of Fuel Performance Modeling using Artificial Intelligence



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First Ever Enriched Uranium Fueled Chloride Salt Irradiation



Abdalla Abou-Jaoude, William Phillips, **Gregory Core, Chuting Tsai**

Project Number: 21A1050-016FP

www.inl.gov

Work supported through the INL Laboratory Directed Research & Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517."

Why?

- Interest is **surging** in Molten Salt Reactors
- **Need** to establish US-based salt irradiation capability
- Irradiating salt will help us understand: **Source term**: where do
 - radionuclides go?
 - **Properties**: do salt properties change with burnup?
 - **Corrosion**: does irradiation affect wall material corrosion rate

Where?

INL's Neutron Radiography Reactor (NRAD)



LRS Number: INL/MIS-23-74314

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What?

0.33 UCl₃ – NaCl at 93wt% 235U





Double-encapsulated temperaturecontrolled experiment vehicle

How?

Under irradiation:

- Fission Heat = 20 W/cm³
- **Neutron Flux** = 3.5×10^{12} n/cm²-s
- Gamma Flux = $1.4 \times 10^{13} \gamma/cm^2-s$
- **Salt Temperature =** 525-900°C



← Inserting the experiment in the reactor

> Simulation of the experiment performance →







Plasticity is harder to catch than you might think...



Single crystal testing helps clarify the confusion

Boone Beauosleil, NS&T INL Co-Pls: N. Cinbiz, Y. Wang, S. Pitts NCSU Co-Pls: D. Kaoumi, M. DeJong, Philip Alarcón-Furman MIT Co-PIs: J. Li, Q. Li

Project Number: 21A1050-060FP

www.inl.gov

Work supported through the INL Laboratory Directed Research & Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517."

System B?

Conceptual Goal of the Project

tests of wrought and singlecrystal anisotropic materials

2. Utilize computational tools to understand and uncertainties











Accelerating Pathways to **Actinide Materials Discovery** Through Combinatorial Deposition



PRESENTER: Brelon May

BACKGROUND

- Global lack of capabilities to fabricate, test, and screen actinides stifle research
- *Transport by design*: What pathways enable key transport properties?
 - Mass and energy
 - Need detailed understanding of correlation between the lattice, phonon, and electrons



- Superconductivity? • Novel Quantum States? Spin-Charge Correlation? Emergent Behavior?
- Building foundational knowledge of thin film deposition for actinides at INL

METHODS

- **Molecular Beam Epitaxy** (MBE)
 - Nitrides at INL
 - III-Vs at

Boise State University Pulsed Laser Deposition (PLD)

- Ln-oxides at University of Utah **Computational modeling**
- Phonon transport of various materials, INL & University of California-Riverside



PLD of Sm₂O₃ Mn & Co alloying properties

Phonon modeling in III-Ns



Project Number: 21A1050-052FP

www.inl.gov

Work supported through the INL Laboratory Directed Research & Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517."

Interfaces change radiation

damage MBE-grown **Bulk material** behaves differently compared to superlattices



Deposition of lanthanide oxides 90 80 % u.) ⁷⁰ و **(**а 90 60 50 sity Inten ₩ 40 30 20 XRD changes optical

250 350 450 550 650 750 Wavelength (nm)

20

Thermal transport in the AlGaN based material system

- First-principles to finite-element
- High power optoelectronics
- Potential radiation-hard sensors

LRS Number: INL/EXP-23-74107

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First growth of GaSb on GaAs (111)



Giant MR in GaSb >150,000%



Phonon property calculations



Papers from this project

- Cody A. Dennett, et al., Nature Comm, 13, (2022)
- Kevin D. Vallejo, et al. **Rep. Prog. Phys**. 85 123101 (2022)
- Madison D. Nordstrom, et al. , Cryst Gro Des. (submitted)
- Gitanjali Mishra, Ashutosh Tiwari, APS March Meeting Abstracts, 2022
- Madison D. Nordstrom, et. al., (in-prep)
- Gitanjali Mishra, et. al (in-prep)
- Jackson Harter, Cameron Chevalier, Alex Greaney (in-prep)
- INL: Cody Dennett, Narayan Poudel, Kevin Vallejo, Jackson Harter, ShuixangC Zhou, Krzysztof Gofryk, Brelon May **UoU**: Gitanjali Mishra Ashutosh Tiwari, **BSU**: Maddy Nordstrom, Paul Simmonds, **UCR**: Cameron xx, Alex Greany **NIST**: Maria Muñoz, Tehseen Adel, Angela Hight Walker





Title: Machine Learning Interatomic Potentials for Radiation Damage and Physical Properties in Model Fluorite Systems

PRESENTER: Chao Jiang

BACKGROUND: Machine learning interatomic potential (MLIP) has emerged as a powerful paradigm-shifting tool for addressing the computational challenge of modeling radiation damage in nuclear materials. In this project, we have developed MLIP to predict the structures and stabilities of small interstitial and vacancy clusters in irradiated ThO₂ with a fluorite structure, which has been proposed as an alternative nuclear fuel. While these small defect complexes are invisible under transmission electron microscopy (TEM), they can significantly downgrade the thermal conductivity of ThO₂ via phonon-defect scattering.

METHODS: A large database containing 3,672 total energies and 3,521,988 atomic forces has been constructed via high-throughput density functional theory (DFT) calculations. A neural network-based MLIP for ThO₂ has been trained using a supervised learning approach.

RESULTS: An exhaustive search for the groundstate (GS) defect structures has been performed using MLIP as a high-fidelity yet low-cost surrogate model for DFT. A total of 10,557,845 defect configurations have been considered. The search leads to many unexpected results such as non-compact GSs and GS polymorphism. The impact of atomic-scale defects on the thermal conductivity of ThO₂ has also been predicted.





Stability of small defect clusters in ThO₂. (a) and (b) show the total binding energies of interstitial and vacancy clusters in their GS configurations. The DFT-calculated incremental binding energies are shown in (c) and (d). The shaded areas indicate the range of total charges (q) where the defect clusters are thermodynamically stable.

Project Number: 21A1050-078FP

www.inl.gov

Work supported through the INL Laboratory Directed Research & Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517."

Ground-state configurations of atomic-scale defect clusters in ThO₂. (a) shows the unexpected non-impact ground-states of small interstitial clusters, while (b) demonstrates the existence of ground-state polymorphs.

LRS Number: INL/MIS-23-74117





3Va_{Th}+6Va_O 8.33 *Experiment data from Acta Mater 213, 116934.

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An Innovative Approach for Accelerated Irradiation Studies of Materials

1. Idaho National Laboratory. 2. Massachusetts Institute of Technology.

Introduction

The objective of this project is to develop an innovative approach to accelerate irradiation studies of materials in nuclear reactors. For many years, ion irradiation has been used as a surrogate for neutron irradiation as the ion flux can be readily tuned to achieve high irradiation flux. However, ion irradiation creates a number of features in materials that are not observed in neutron irradiated specimens, such as irradiation polarization artifacts, defects imbalance, etc. We propose to develop a new approach to accelerate irradiation damage studies of materials in nuclear reactors using Boron neutron capture (BNC) approach.

Materials, methods, and results

Titanium-aluminum-tungsten-boron (Ti-Al-W-B) alloys have been fabricated using spark plasma sintering (SPS) process under 50 MPa at 1375°C. The alloys were irradiated in NRAD reactor and the post-irradiation examination was performed using transmission electron microscopy at IMCL at INL.



Figure 1. Neutron irradiation in NRAD reactor at INL. (a) Fabricated wet tube and smallscale J-type specimens. (b) The position (red spot) of the loaded capsule in the reactor. (c) Schematics of irradiation capsule and its irradiation location.

Project Number: 21A1050-099FP

www.inl.gov

Work supported through the INL Laboratory Directed Research & Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517."

Cheng Sun¹, Mukesh Bachhav¹, Chao Jiang¹, Ju Li²

Figure 2. Chemical distribution of Ti-Al-W-B alloy. (left) Before irradiation. Ti-Al alloys showing two-phase nano-lamellar structure with Mo segregated in the α phase. (right) After neutron irradiation. Irradiation-induced intermixing occurs at such low dose irradiation due to the accelerated irradiation flux caused by boron addition. Mo is uniformly distributed in both α and β phases after irradiation.

Conclusions and impact

This project used the concept of BNC therapy to accelerate in-pile irradiation damage in research reactors. By using this approach, the desired irradiation doses can be achieved with much shorter time and lower cost. This approach dramatically decreases the cost and time required for irradiation testing in reactors and expedite the qualification of new nuclear materials and validation of computational models.

Publications

- *Materials Sciences,* 26, 2022, 100975.

LRS Number: INL/EXP-23-74104

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Pristine microstructure

Irradiation-induced intermixing



H. Xu, S. Kim, D. Chen, J. Monchoux, T. Voisin, C. Sun, J. Li, Advanced Science, 32, 2022, 2203555.

D. Morgan, G. Pilania, A. Couet, B. P. Uberuaga, C. Sun, J. Li, Current Opinion in Solid State and





In-situ Positron Annihilation Spectroscopy

Chuting Tsai, Jagoda Urban-Klaehn, Chase Taylor, Connor Harper

Motivation

- PAS is sensitive to low vacancy concentration (~10¹⁴ cm⁻³) and small defect size (sub nanometer). It can probe the formation of vacancy defects well below 1 dpa.
- Experimentally observe the generation and the evolution of point defects by probing the size, density and type of the vacancy type of defects.



Method development - Experiment

Method development - Software



b)

a)

Research Outputs

- Method for neutron source activity determination
- Optimization of n, y reaction
- Accurate detector efficiency determination

Experiment theoretical

High Energy Neutron Flux



Research Outputs

- Open-source software
- Versatile, transparent, and fast Coincidence Doppler Broadening data analysis tool

Design and results





Rate (Hz Gadolinium Oxide **Borated Poly** Tungsten 10 1500 2000 1000 Energy (keV) **Research Outputs** Drawings released for NRAD, experiment at university assembled Binned data would indicate hourly evolution of defects Coincidence rate 157hz at NRAD, 2.9hz at OSURR Reference and acknowledgement

- Howell, Richard H., Thomas E. Cowan, Jay H. Hartley, and Philip A. Sterne. "Positron beam lifetime spectroscopy at Lawrence Livermore National La Conference Proceedings, vol. 392, no. 1, pp. 451-454. American Institute of Physics, 1997.
- Positron Annihilation at Martin-Luthen-University Halle: http://positron.physik.uni-halle.de/
- Stonaha, P. J., C. Harper, C. Tan, J. Urban-Klaehn, C. N. Taylor, T. Forest, and D. Dale. "Accurate activity determination of a californium neutron source." Applied Radiation and Isotopes 194 (2023): 110712.
- Evans, George S., Joseph M. Watkins, Chase N. Taylor, Jagoda Urban-Klaehn, and Chuting T. Tsai. "CDB-AP: An application for coincidence Doppler broadening spectroscopy analysis." SoftwareX (2023): 101475.
- Work supported through the INL Laboratory Directed Research& Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517



(505keV < E < 517keV)



An accelerated assessment of the creep mechanisms in uranium zirconium model alloys

Principal Investigator: David Frazer, Co-PIs: Dewen Yushu, Tianyi Chen Contributors: Tzu-Yi Chang, Gavin Vandenbroeder, Stephanie Pitts

Creep in nuclear fuel

Creep is generally observed in nuclear fuel, cladding, and structural materials. It limits the lifetime of the nuclear components. Various factors such as high temperature, stress, irradiation, and the material microstructure evolution, simultaneously complicate the deformation mechanism behind the creep phenomena. Thus, understanding the creep on fuel and structural materials in a nuclear reactor is essential for safe reactor operation but remains challenging.

Challenges

Conventional measurements are expensive and time creep consuming. This makes it difficult to gather data quickly and efficiently for new structural and fuel material development. In addition, the microstructural heterogeneity in irradiated fuels prevents conventional testing methods to obtain microstructuredependent creep properties.

Nanoindentation method

With a smaller amount of sample, nanoindentation creep measurements hold promise as they have been shown to measure the creep stress exponent that is comparable to the macro-scale values but at a significantly reduced time scale. It also gives localized material information regarding a specific area of interest.

Significance

This project combined modeling and nanoindentation creep measurements to better understand the deformation that is taking place under the tip. Specific areas of interest are the examination of the interface between plastic deformation and elastic deformation regions under the indent.

The understanding of the size of the plastic zone and its growth as compared with the elastic zone during the indent would give insights into the deformation process taking place in the material.

Creep test

- (1) Annealed U-50 wt% Zr samples were polished to a mirror finish for the nanoindentation creep test in vacuumed SEM chamber.
- (2) Nanoindentation creep tests were conducted with a Berkovich tip under the force-controlled mode.
- (3) The force dependency, temperature dependency, and loading rate dependency were examined.
- (4) The data was processed with classic creep theory.

Stress relaxation test

- (1) The stress relaxation tests were conducted with a Berkovich tip under the displacement-controlled mode.
- (2) Stress relaxation tests were performed on both U-50Zr and purealuminum.
- (3) The data was processed with power law and general-Maxwell models.

Computational modeling

- (1) Modeling and simulation of the indentation process are carried out using MOOSE [1] and the mesoscale code, Marmot [2], for the aluminum and alpha uranium crystal plasticity capabilities, respectively.
- (2) The modeling visualized the microstructural evolution and stress distribution under the Berkovich tip.



Project Number: 22P1068-002FP

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Work supported through the INL Laboratory Directed Research & Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517."

Methodology

[2] Idaho National Laboratory, Virginia Polytechnic Institute and State University "MARMOT Mesoscale Simulation Code" https://inlsoftware.inl.gov/product/marmot

Creep is a time-deformation phenomenon that can relate to stress, temperature, and microstructure. The stress exponent based on the classic creep theory is an experimental value of stress sensitivity used to infer a possible mechanism and structural evolution of the deformation. Our results show a force effect, temperature effect, and loading-rate effect on creep behavior via nanoindentation method.



Stress relaxation is a phenomenon of atom re-arrangement during material deformation. Our results from both experiment and modeling show a loading rate dependency on stress relaxation, and a new approac for stress sensitivity estimation is developed.

LRS Number:

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Nanoindentation creep was demonstrated on nuclear fuel materials up to 200°C. Temperature dependency of the obtained creep exponent was observed, agreeing with the creep theory. The load-dependency and stress relaxation were also identified for future investigation.

Creep

Stress Relaxation

was simulated using MOOSE with crystal plasticity model (c) and the relationship between stress relaxation and pre-loading rate is demonstrated as a new approach for stress exponent estimation (d).

INL/EXP-23-74126



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Modeling and Separate Effect Tests to investigate the microstructure of at the top of metallic fuel pins



The porous (*fluff*) structure at the top of the metallic fuel pins may influence reactivity and the source term.



METHODS

- 1. Review of available database to develop correlations.
- 2. Image analyses to avoid subjectivity.
- BISON simulation to provide insight on the phenomena.
- 4. Separate effect test for creep and thermal gradients.

RESULTS

- Quantified relations between fluff length and fuel parameters/irradiation conditions.
- Developed an image analysis method using new parameters to describe the fluff.
- Modelling indicates the source of this structure to be Fuel/Cladding Mechanical ilnteraction or fission gas and porosity growth.
- Creep Separate Experiments show that current models are unable to simulate this structure.
- Developed a furnace with prototypical temperature gradients and sodium cooling.





Project Number: 21A1050-006FP

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Work supported through the INL Laboratory Directed Research & Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517."

The fluff length has a direct relation to burn-up, temperature and fuel composition.

LRS Number: INL/EXP-23-73840

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| Property | Description | | |
|---|--|--|--|
| Total area of the porous matter, cm ² | Calculates the total number of pixels in all | | |
| | porosity regions and converts the number to | | |
| | cm^2 . Measures the total amount of porous | | |
| | matter present for each pin. | | |
| Total convex area of the porous matter, cm ² | Calculates the area of the smallest convex | | |
| | polygon containing all porosity regions, called | | |
| | convex hull. Measures the dispersion of the | | |
| | porosity for each pin. | | |
| Solidity, unitless | Total area/total convex area, calculates the | | |
| , | ratio of the porous matter area within the | | |
| | convex hull to the area of convex hull. | | |
| | Solidity is bounded from above by one. | | |
| Average extent, unitless | Total area/region's bounding box area, extent | | |
| ;;; | is bounded from above by one. Measures the | | |
| | density of the porous matter region within its | | |
| | bounding box. | | |
| Average eccentricity, unitless | Eccentricity measures the average | | |
| g,, | roundedness of the porosity regions. For a | | |
| | single region, the eccentricity is equal to 0 if | | |
| | the region is a perfect circle, and it is 1 if the | | |
| | region is a line segment. The eccentricity and | | |
| | average eccentricity are between 0 and 1. | | |
| Average equivalent diameter, cm | Diameter of a circle with the same area as a | | |
| | porosity region averaged over all regions | | |
| | within bounding box. Measures granularity of | | |
| | the porous matter. | | |
| Average perimeter, cm | Measures perimeter of each porosity region | | |
| | for a pin and takes the average. | | |



OUTCOMES

5+ journal papers and 1 graduate fellow







Project Number: 21A1053-007FP



Work supported through the INL Laboratory Directed Research & Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517."

LRS Number: INL/EXP-23-74083

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SCAN ME



► 6 open-source software tools Supports ongoing efforts

Visualization 3

- Human-centered
- Real-time data and alerting
- Scalable and interactive



4 Automated Control

Predictions of heat pipe state used to avoid undesirable states or anomalies before they occur







PRESENTER:

Kyle A. Gamble

Modeling and Measurement of Axial Gas Transport in Nuclear Fuels



Project Number: 21A1050-028FP

www.inl.gov

Work supported through the INL Laboratory Directed Research & Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517."

PI: Kyle A. Gamble

Co-Pls: Fabiola Cappia, Seongtae Kwon, Chase Christen, Kaustubh Bawane, Chiara Genoni, Tommaso Bergomi

Main Research Findings

Scalability of axial gas transport confirmed More accurate fracture patterns obtained by quenching Pressure equilibration is not instantaneous Gas flow is turbulent for short decay times Permeability equation developed as a function of smeared **porosity** obtained from image analysis



Figure 3: a) Thermal quench (top view) b) thermal quench (side view), c) mechanical crushing, and d) experimental micrograph of irradiated fuel



 ϵ_s = smeared porosity $\mu = dynamic viscosity$ $C_1, C_2 =$ pressure-dependent constants



Figure 5: Best-fit curves excluding the Forchheimer coefficient for experiment CT4 at different pressure levels



Figure 6: Snapshots of computational fluid dynamicssimulation of CT4 with initial pressure of 4.3 MPa

Publications

[1] C. Genoni, et al., "Modeling and Measurement of Axial Gas Transport in Nuclear Fuels," ANS Annual Meeting, June 2023. [2] S. Kwon, et al., "Fabrication of Surrogate Oxide Spent Fuel with Various Cracking Patterns and the Design of an Axial Gas Transport Apparatus," to

[3] C. Genoni, et al., "Investigation of the Impact of Non-Uniform Permeability on Axial Gas Transport within Light Water Reactor Fuel Rods during a Loss-Of-Coolant Accident," to be submitted to Nuclear Engineering and Design.

[4] T. Bergomi, "Fuel Pellets Three-Dimensional Properties Reconstruction Exploiting Image Analysis: A Bridge Between Experiments and Modeling",

LRS Number: INL/MIS-23-74111

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Turbulent **Friction Factor** (Forchheimer's Term)

 $\overline{u} =$ velocity $\rho = \text{density}$

Specimen Fabrication and Experimental Apparatus

- Decay of inlet pressure measured as a function of time
- 4.3, 5.6, and 7 MPa analyzed Quenching and mechanical crushing used to induce fracture
- Mylar wrapping used to preserve pellet position







Figure 7: Photo of (a) pellets with mylar wrapping, (b) mechanical compression of individual pellet, and (c) resulting separation-crack formation

Digital Image Analysis

- Hundreds of two-dimensional (2D) images obtained per specimen by x-ray computed tomography (CT)
- Image analysis used to estimate features
 - Crack tortuosity
 - Specific surface
 - Porosity distribution
- **3D reconstruction** of the pellets can be performed





Figure 8: CT slice (top), 3D reconstruction (bottom)

References

- [1] V. Rondinella et al., TopFuel 2015. JRC94524.
- [2] W. Wiesenack, et al. International Conference on the Physics of Reactors, 2008.
- [3] R. Montgomery and R. N. Morris, doi: doi.org/10.1016/j.jnucmat.2019.05.041.
- [4] S. J. Dagbjartsson, et al., TREE-NUREG-1158, 1977.
- [5] Khvostov, G., et al., doi: doi.org/10.1016/j.nucengdes.2011.03.003.

Acknowledgments

- William Chuirazzi for performing the x-ray CT of the specimens
- Fei Xu for supporting the digital image analysis
- Davide Pizzocri (Politecnico Di Milano) for modeling discussions
- This research made use of the resources of the High Performance Computing Center at Idaho National Laboratory, which is supported by the Office of Nuclear Energy of the U.S. Department of Energy and the Nuclear Science User Facilities under Contract No. DE-AC07-05ID14517.



during a simulated loss of coolant accident (LOCA)



PRESENTER:

Ahmed Hamed

BACKGROUND:

Reactor vendors seek economic benefits associated with increasing nuclear fuel service lifetime in the existing light-water reactors fleet. FFRD phenomena represent a major safety concern which still needs to Before fuel stack Crumbling and axial be addressed. Formation of high burnup structure (HBS) in conjunction with LOCA can lead to relocating fuel to escape the fuel pin and get dispersed into the primary coolant system.

METHODS

- 1. BISON is used to simulate experimentally observed scenarios leading to FFRD.
- 2. BISON-informed Discrete Element Method is used to simulate FFRD dynamics and analyze controlling parameters.



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Project Number: 22P1074-009FP

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Work supported through the INL Laboratory Directed Research & Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517."

FFRD schematic is adopted from Siefken, Int. Conf. on Structural Mechanics in Reactor Technology, 1983

High-fidelity multiscale model development for accelerated fuel qualification for high discharge burnup Finite element-informed, discrete element modeling of fuel fragmentation, relocation, and dispersal (FFRD) phenomena



LRS Number: INL/MIS-23-74169

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Modeling Flow-Informed Corrosion in Molten Salts Poisson-Nernst-Planck Model

PI - Mauricio Tano (C130); Co-PIs: Samuel Walker (C120) & Abdalla Abou-Jaoude (C120)



www.inl.gov



Experiment: Raiman, S. S., Kurley, J. M., Sulejmanovic, D., Willoughby, A., Nelson, S., Mao, K., ... & Pint, B. A. (2022). Corrosion of 316H stainless steel in flowing FLiNaK salt. Journal of Nuclear Materials, 561, 153551.





- Further validation of the model and transition to programmatic and vendor usage of the model

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Scaling, Validation and Uncertainty Characterization 💑 🍝 Mohammad Abdo (PI), Congjian Wang (CoPI), Aaron Epiney (CoPI), Ramon Yoshiura, Botros Hanna, Alexander Duenas, Charles Folsom, and From Purdue University: Shiming Yin, Hany S. Abdel-Khalik (CoPI)

METHODS

BACKGROUND

- Code/model validation, Scaling, and Uncertainty Characterization are indispensable for Nuclear Digital Transformation.
- Quantitatively judge the relevance (representativity) of a prototype model to a full target model.
- Qualify experiment(s) *before* execution and design better experiments, lower cost, hence less destructive experiments.
- Parameter adjustment/calibration based of training models to reduce uncertainties for Reactivity Insertion Accidents (RIAs).

CONCLUSIONS

- Three theories: **representativity**, **PCM**, and **DSS** were compared for model validation.
- Representativity performed the best in case global sensitivities are present.
- Representativity and PCM can qualify experiments, based on reduction in Uncertainty.
- DSS shows the **global distortion** in the dimensionless transformed space and guide the judgement whether the models are ill-scaled or







Project Number: LDRD 21A1050-014FP



Work supported through the INL Laboratory Directed Research & Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517."

Representativity



LRS Number: **INL/MIS-23-74350**

Physics-guided Converged Mapping



Dynamic System Scaling

$$\beta(t) = \frac{1}{\Psi_0} \iiint_V \Psi(\vec{x}, t) dV$$
$$\omega(t) = \frac{d\beta}{dt} \Big|_t = \sum_{i=1}^n \omega_i , D = -\frac{\beta}{\omega^2} \frac{d\omega}{dt}, \tau_s = \int \widetilde{\Omega} = \omega \tau_s , \tilde{\beta} = \beta , \tilde{t} = \frac{t}{\tau_s} , \tilde{D} = D$$





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BACK TO THE FUTURE: HYDRIDE MODERATORS

Idaho State University

BACKGROUND: Use of Solid Metal Hydride Moderators Allow Compact Transportable **Nuclear Reactors**



Elevated Temperatures (>500°C) For 10 **Years of Operation**



H redistribution due to ∇C and ∇T

SOLUTION: Hydride Moderator Design Via Computations \leftrightarrows Experiments



Project Number: 21A1050-020FP

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Work supported through the INL Laboratory Directed Research & Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517."

Presenter: M. Nedim Cinbiz (PI), Co-PI: Jianguo Yu Content Collaborators: A. Sundar, Li Qi (UM), Y. Huang, J. Eapen (NSCU), T. Lach, E. Cakmak, A, Le Coq, K. Linton (ORNL) LDRD Co-Pls: C. Taylor, D. Labrier (ISU), M. Short (MIT)

METHODS: Electronic structure Hydrogen Diffusional Characteristics Alloying Irradiation

Density Functional Theory+ Ab Initio Molecular Dynamics+ Gaussian Potentials + Kinetic Monte Carlo + Incoherent Quasi Elastic Neutron Scattering + Transmission Electron Microscopy

1. HYDROGEN RETENTION IS GOVERNED BY CHARGE TRANSFER FROM HOST OR ALLOYING ELEMENT TO HYDROGEN, CHARGE LOCALIZATION, & METALLICITY

Pure Yttrium Hydride



IQENS Results (Spallation Neutron Source)



2. NANO-SCALE CAVITIES ACT AS STORAGE POCKETS WHICH REGULATES THE HYDROGEN

LRS Number: INL/MIS-23-74174

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OAK RIDGE National Laboratory

Binary Alloy Hydride





Accelerating Rare Events Estimation for the Safety Evaluation of Advanced Reactor Technologies

TEAM: Som Dhulipala, Ben Spencer, Vincent Laboure, Zach Prince, Peter German, Yifeng Che, Mike Shields, Promit Chakroborty, Denny Thaler

BACKGROUND: Safety evaluation of advanced reactors is computationally very expensive (failure probabilities b/w 1E-4 to 1E-8). This project employed ML-enabled UQ methods to significantly reduce this computational burden. Results will positively impact the safe design and optimization of advanced reactors.

DEVELOPED COMPUTATIONAL METHODS

- 1. Multifidelity modeling in active learning
- Control variates importance sampling Uncertainty quantification with 3. Hamiltonian Neural Networks

APPLICATIONS AND RESULTS

- **TRISO fuel, reactor pressure vessel** embrittlement, and heat-pipe reactor Developed methods accurately estimated very rare events (failure
- probability: 1E-4 to 1E-8) Computational effort reduced by 3 orders of magnitude compared to state-of-practice.



OPyC SiC IPyC Buffer Kernel

Project Number: 21A1050-114FP

RINT AACHEN

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JOHNS HOPKINS

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importance sampling

UQ with Hamiltonian Neural Networks



LRS Number: INL/MIS-23-74133

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OUTCOMES

PUBLISHED/ACCEPTED JOURNAL PAPERS

- "Active Learning with Multifidelity Modeling for Efficient Rare Event Simulation" Journal of Computational Physics
- "Accelerated Statistical Failure Analysis of Multifidelity TRISO Fuel Models" Journal of Nuclear Materials
- "Reliability Estimation of an Advanced Nuclear Fuel using Coupled Active Learning, Subset Simulation, and Multifidelity Modeling" *Reliability* Engineering & System Safety
- "General Multi-Fidelity Surrogate Models: Framework and Active Learning Strategies for Efficient Rare Event Simulation" Journal of Engineering Mechanics
- "Efficient Bayesian Inference with Latent Hamiltonian Neural Networks in No-U-Turn Sampling" Journal of Computational Physics

JOURNAL PAPERS UNDER SUBMISSION

- "Parallel Uncertainty Quantification in MOOSE: Forward, Bayesian Inverse, Active Learning, and Multifidelity Modeling Capabilities" Journal of Computational Science
- "Reliability Analysis of Complex Systems using Subset Simulations with Hamiltonian Neural Networks" *Structural Safety*
- "A Coupled Control Variates and Importance Sampling Method for Efficient Bifidelity Reliability Analysis" SIAM/ASA Journal on Uncertainty Quantification

SOFTWARE DISCLOSURE RECORD

BIhNNs: Bayesian Inference with Neural Networks (CW-22-35)

TALENT PIPELINE

Yifeng Che (Russell Heath Distinguished Postdoc), Promit Chakroborty (Outstanding Contribution Prize), Eusef Abdelmalek (GEM Fellow), Akram Batikh

AWARDED GRANT PROPOSALS

- DOE Nuclear Safety Research & Development (NSR&D) Program
- DOE Nuclear Energy University Partnerships (NEUP)

FOLLOW-ON FUNDING FROM PROGRAMMATIC ACTIVITIES

- DOE Nuclear Energy Advanced Modeling and Simulations (NEAMS)
- **DOE Advanced Materials and Manufacturing** Technologies (AMMT)



Simulating Hydrogen Migration for Microreactor Applications using MOOSE-Based Tools Stefano Terlizzi¹ (PI), Mark DeHart¹ (co-investigator), Vincent Labouré¹, Quentin Faure²

1. Reactor Physics Methods and Analysis Group, Idaho National Laboratory, 1955 N Fremont Ave, Idaho Falls, ID 83415 2. Department of Nuclear Engineering, North Carolina State University, 2500 Stinson Drive, Raleigh, NC 27695

Introduction

The introduction of nuclear microreactors is projected to open new markets for the nuclear power industry because of potential to be cost-competitive in non-traditional market segments. An obstacle to the deployment of many nuclear microreactor concepts is their reliance on high-assay low-enriched uranium (HALEU). In fact, despite enabling the design of compact systems and long operational lifetime, usage of HALEU entails both technical and regulatory challenges. Reduction of the fuel enrichment or quantity while maintaining the design compactness and high operating temperature can be achieved by using metal hydrides. However, it has been shown that the hydrogen contained in the hydrides tends to redistribute and leak from the moderating elements leading to reactivity losses, and, potentially, failure of the moderating elements, with consequent reactor shutdown.

This work aimed at (1) modeling the hydrogen migration in hydrides, with emphasis on yttrium hydride, in the Multiphysics Object-Oriented Simulation Environment (MOOSE). (2) Gaining a better understanding on the effect of hydrogen migration on neutronics and thermal field in prototypical nuclear microreactors, and (3) **Perform a rigorous uncertainty** quantification to assess experimental needs.

Theory

Three sub-phenomena determine the hydrogen migration in metal hydrides: (a) Hydrogen redistribution of the hydrogen in the hydride's bulk is driven by the temperature and hydrogen concentration spatial gradients.

$$\frac{dc_H}{dt} = \nabla \cdot \left(-D\left(\nabla c_H + \frac{Qc_H}{R T} \nabla T \right) \right).$$

(b) Hydrogen dissociation at the hydrogen surface due to material-dependent adsorption-desorption dynamics.

$$J_H^s \cdot \vec{n} = J_{des} - J_{ads}.$$

(c) Leakage through the clad surrounding the hydride can be computed through the permeability ϕ and the partial pressure of hydrogen p_H given by the pressureconcentration-temperature (PCT) curves:



Publications

(2)

[5] Faure Q., Labouré, V. Terlizzi S. (Expected Submission Date: 20 November 2023). Multi-Physics Uncertainties Quantification on [3] Terlizzi S. and Labouré, V.(2023) Asymptotic Hydrogen Redistribution Analysis in Yttrium Hydride Moderated Heat-pipe-cooled [1] Terlizzi S., Labouré, V., and DeHart M. (2022). Preliminary Observations on the Hydrogen Redistribution Feedback in Neutronics Response for a Prototypical Yttrium-Hydride Moderated Heat-Pipe-Cooled Microreactor, Annals of Nuclear Energy Microreactors using DireWolf, Annals of Nuclear Energy. YH-Moderated Monolithic Microreactors. 2022 ANS Annual Meeting [6] Terlizzi S., Faure Q., (Expected Submission Date: 30 October 2023) On the effect of hydrogen dissociation on the lifetime of hydride-[4] Faure Q., Labouré, V., and Terlizzi S. (2023) Preliminary Results for Uncertainty Quantification on Asymptotic Hydrogen [2] Terlizzi S., Labouré, V., and DeHart M. (2022). Selected results from full-core hydrogen redistribution asymptotic moderated nuclear microreactors, Physor 2024, April 2024. Redistribution in a Prototypical Yttrium-Hydride Moderated Heat-Pipe-Cooled Microreactor, ANS Winter Meeting, Washington DC, analysis in YH-moderated heat-pipe cooled microreactor. 2022 ANS Winter Meeting. USA, November 2023.

Project Number: 21P1056-010FP

www.inl.gov

Work supported through the INL Laboratory Directed Research & Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517."

Test Problem



problem named the Simplified Microreactor Benchmark Assessment (SiMBA) problem was prepared as a prototypical heatyttrium hydride-moderated cooled The coupled neutronic, heat microreactor. thermal-hydraulics, hydrogen conduction, redistribution equations were solved for the full reactor.

The details of the design were made generic enough to avoid any proprietary concerns, but specific enough to capture the primary design characteristics of the envisioned HP-cooled monolithic microreactors. A model based upon will be included on the Virtual Test Bed (VTB) by the end of the fiscal year.

Redistribution



965.0 965.0 955.0 955.0 945.0 945.0 945.0 930.0 930.0 930.0 930.0 930.0 930.0 930.0

The hydrogen redistributes towards colder zones. The sign of the feedback is negative due to the migration of the hydrogen toward colder axial zones. These axial zones are associated with low neutron usually importance, thus leading to a negative effect on reactivity. The magnitude of the feedback was found to be on the order of -29 pcm on the effective multiplication factor for the SiMBA reactor.

Dissociation

Experimental set-up: Pure yttrium samples (0.142 cm x 1.27 cm x 1.3 cm) are inserted into a reaction tube with fix temperature (no gradient of temperature) and pressure. Adsorption of hydrogen into the yttrium is measured.

Models for hydrogen dissociation of hydrogen at the yttrium hydride surface, including desorption, adsorption and were implemented in Bison and the results obtained were compared to the experimental values.

The solid line are Bison and the crosses are experimental values.



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Leakage

The leakage through 500-μm thick SS-3316 clad was simulated using the permeability-based equation in Bison. Two different PCT curves were used to implement the hydrogen leakage in Bison.

Average hydrogen stoichiometric ratio for the yttrium hydride pins in the SiMBA problem were calculated against time for 10 years operation at 870 K, showing the non-negligible decrease in hydrogen content over the MR lifetime. Additionally, the leakage is strongly dependent upon the model used for the PCT curves.

JQ

To obtain information on the impact of uncertain inputs on the temperature and H/Y ratio distribution, we rely on the two-step approach. The methodology allows to consider the different nature of the uncertainties (epistemic vs. aleatoric).

It was found that the magnitude of the epistemic uncertainty of the heat of transport shadows the influence of the aleatoric uncertainties.







Conclusions

- (1) The hydrogen redistribution equation was solved in Bison. The effect of the hydrogen redistribution on the power density, eigenvalue, and temperature was then obtained by coupling the Bison inputs with full core neutronic and heat transfer models developed within the Direwolf software driver. It was found that the feedback is negative due to the redistribution of hydrogen towards colder zones, usually associated to lower importance zones.
- (2) A model describing hydrogen adsorption-desorption and leakage for yttrium hydride was implemented. It was shown that the results are extremely sensitive to the model used to describe the current at the hydride's boundary. This uncertainty may affect estimations of the MR's lifetime non-negligibly.
- (3) The UQ analysis confirmed the importance of obtaining a reliable experimental value for the heat of transport in order to accurately quantify the effect of hydrogen redistribution in yttrium hydride on neutronics.



Quantitative Reliability Analysis for Unattended **Operation of Fission Batteries**



PRESENTER: Steve Prescott

BACKGROUND: Autonomous controlled, "Plug & Play" fission battery concepts are difficult to model and analyze. These highly Cyber-Physical system need more than classical risk analysis to handle the desired safety and business cases. Dynamic probabilistic risk assessment (PRA) is promising but has limitations, many of which can be overcome. **METHODS**

- Dynamic PRA tool EMRALD
- Coupled dual-graph error propagation methodology (DEPM) tool OpenEPL

DEPM

Classic

PRA

RESULTS

- Cyber protection modeling with reactor behavior
- Complex time scenarios for automated safety control
- Compare operator vs. autonomous

Nodel and analyze complex Cyber-Physical system interactions



Dynamic PRA

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Work supported through the INL Laboratory Directed Research & Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517."











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Papers

A combined strategy for dynamic probabilistic risk assessment of fission battery designs using EMRALD and DEPM

Probabilistic Methods for Cyclical and Coupled Systems with Changing Failure Rates

Introducing Multiple Control Paths in the Dual Error Propagation Graph for **Stochastic Failure Analysis of Digital Instrumentation and Control Systems**

LRS Number: INL/MIS-23-73993

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Communication and automation diagram to identify modeling areas and boundaries.



EMRALD model showing the states of a core drum.



Dynamic analysis (purple) vs. standard failure outcomes.



Sankey visualization results for failure paths and timing.

Steven Prescott, Arjun Earthperson, Jooyoung Park, Thomas Ulrich, Mihai Diaconeasa Bri Rolston, Troy Unruh, Jisuk Kim





Characterizing corrosion mechanisms of structural alloys in actinide-based molten chloride salt

- Trishelle Copeland-Johnson¹, Michael Woods¹, William C. Chuirazzi¹, Ruchi Gakhar¹,
- Daniel J. Murray¹, Guoping Cao¹

¹ Idaho National Laboratory, 1955 N. Fremont Ave. Idaho Falls, ID 83415

Motivation

The corrosion performance of structural materials in contact with molten salts for closed fuel cycle applications, such as electrorefining and molten chloride salt fast reactors, are of concern.

Methodology – Correlated Multi-Modal Advanced Characterization





Automated 3D thickness measurement : 123.80 µm ± 15.00 µm





TEM Microscopy Results

TEM Lamellas from Corroded A617

Site B: Elemental Analysis

Site B: Electron Diffraction











Work supported through the INL Laboratory Directed Research & Development (LDRD) Program under DOE Idaho Operations Office Contract DE-AC07-05ID14517





Scalable Framework of Hybrid Modeling with Anticipatory Control Strategy for **Autonomous Operation of Modular and Microreactors**

Vivek Agarwal (PI), Linyu Lin, Joseph Oncken, Ronald L. Boring, Andrei Gribok, Cody Permann (NS&T); Shannon Eggers (NH&S); and Timothy McJunkin (EES&T)

Objective:

Develop and validate a scalable hybrid modeling and anticipatory control techniques to enable faster than real-time prediction and decisionmaking capabilities for microreactor control.

Technical Approach:



Project Number: 21A1050-067FP

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Demonstration Scenarios and Simulation Results:

Licensed Software: Autonomous **Control fOr Reactor techNologies**

- **National Reactor Innovation Center**
- **Nuclear Energy Advanced Modeling**
- Westinghouse, Ultra Safe Nuclear **Corporation, Pathfinder Energy**



Salient Features of ACORN:

- System Stability robust against sensor drifts/noises, cyber incidents, and failed components.
- Adaptive utilize artificial intelligent algorithms with transfer learning and online updating.

Path Forward and Impact:

- reactor operation.

LRS Number: INL/MIS-23-74179

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 Load-following during normal and abnormal conditions. • Autonomous operations at steady states and power transients. • Adaptive MPC (A-MPC) configurations based on diagnosis results.

• Situational Awareness – utilize design principals from human factor engineering aspects and regulatory guidance.

Demonstrate ACORN to other microreactor stakeholders and quantify uncertainties to build confidence in autonomous controls. A first-of-a-kind ability to advance level of autonomy of nuclear



Accelerate Utilization of **Nuclear Fuel Performance Modeling**

TEAM:

Yifeng Che, Ryan Stewart, Som Dhulipala, Wen Jiang, James Tompkins (X-energy)

ACKNOWLEDGEMENT:

Mengnan Li, April Novak (ANL), Zachary Prince, Peter German, Casey Jesse, Mohammad Abdo

BACKGROUND:

Nuclear fuels undergo complicated thermomechanical-chemical degradation in reactor environment, posing constraints to reactor operation and design. This projects accelerates the utilization of fuel performance modeling by (1) improving the reliability of fuel performance models via inverse uncertainty quantification (UQ), and (2) integrate high-fidelity Bison fuel performance simulation into the multiphysics framework.

JOURNAL PAPERS UNDER PREPARATION:

- A Review and Outlook for Bayesian Analysis in Modeling and Simulation in Nuclear Engineering
- Coupling high-fidelity fuel performance modeling into the multiphysics simulation of high temperature gas-cooled microreactor

Project Number: 22P1066-005FP

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Inverse UQ with Constraints: Spherical Hamiltonian Monte Carlo

Bayesian inference confined to constrained domains is challenging for commonly used sampling algorithms. Boundary conditions handled implicitly via spherical measures in the computational efficient framework Hamiltonian Monte Carlo (HMC). Proposed samples are generated on the sphere that remain within boundaries when mapped back to the original space. Hamiltonian Neural Networks (HNNs) with HMC and No-U-Turn Sampler (NUTS) are integrated with spherical measures for enhanced efficiency.



Multiphysics Coupling: TRISO fuel compact in HTGR

Integrate high-fidelity fuel performance modeling (Bison) into the multiphysics simulation under the MOOSE framework. Allows for high-fidelity simulation of fuel mechanics, failure risks and fission product transportation for steady state and long-term transient.

LRS Number: INL/EXP-23-74268

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| | Algorithm | Min ESS | Max ESS | Accept Rate | Dimension | |
|---------------------------------|----------------|---------|---------|-------------|-----------|--|
| etropolis- astings | RWM (discard) | 12.64 | 45.56 | 0.930 | 2 | |
| onian Monte Carlo (HMC) | HMC (discard) | 523.56 | 873.00 | 0.101 | 2 | |
| | Wall HMC | 2715 | 8293 | 0.981 | 2 | |
| | Spherical HMC | 3079 | 6692 | 0.944 | 2 | |
| urn Sampler NUTS) | NUTS (discard) | 398.90 | 931.26 | 0.214 | 2 | |
| | Spherical NUTS | 4543 | 4700 | / | 2 | |
| onian Neural etwork (HNN) | HNN (discard) | 989 | 989 | 0.099 | 2 | |
| | Spherical HNN | 5744 | 7271 | 0.933 | 2 | |
| *ESS: Effective Sample Size | | | | | | |

Application: **TRISO** in AGR-1

